

Numerical Study of the Effect of the Reynolds Numbers on Thermal and Hydrodynamic Parameters of Turbulent Flow Mixed Convection Heat Transfer in an Inclined Tube

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A numerical investigation of the effect of the Reynolds number on the thermal and hydrodynamic parameters of mixed convection heat transfer of the water- Al_2O_3 nanofluid turbulent flow in an inclined circular channel is the subject of this article. The upper wall of the channel was under non-uniform heat flux and its lower part was isolated. The two-phase mixture model, the finite volume method, and the second-order upstream difference scheme were used to solve the governing equations. After reviewing the results, it was found that by increasing Reynolds number, the convective heat transfer coefficient and shear stress increase, but the surface friction coefficient decreases. In the case of Nusselt number and the surface friction coefficient, some equations were extracted.

Keywords: mixed convection, inclined channel, turbulent flow, Reynolds number, surface friction coefficient

Highlights

- New correlations are proposed to calculate the Nusselt number and surface friction coefficient in an inclined tube which is a function of the Reynolds number and the angle of the tube from the horizon surface.
- The convective heat transfer coefficient increases with the increase of Reynolds number in an inclined tube.
- In an inclined tube, the surface friction coefficient of the length tube decreases when the Reynolds number is increased.
- By increasing volume fraction of the nanoparticles in an inclined tube, the convection heat transfer coefficient is increased.

0 INTRODUCTION

Convective heat transfer in inclined tubes has long been considered. One of the most important applications of the inclined tube is their use in solar collectors and refrigerant distillation in condensers of heat transfer systems [1] to [3], since introducing the subject of adding nanoparticles to the base fluid to improve the efficiency of heat transfer systems, extensive studies were done both numerically and experimentally in horizontal tubes with different boundary conditions and various cross sections [4] to [6]. Saha and Paul [7] studied numerically turbulent flow forced convection heat transfer of two nanofluids and concluded that by increasing the Reynolds number, the Nusselt number increases. Azmi et al. [8] investigated experimental convection heat transfer of nanofluids turbulent flow under constant heat flux of the wall in a circular tube and indicated that the convection heat transfer coefficient increases with increasing the Reynolds Numbers in different volume fractions. Forced convective heat transfer of the water/ Al_2O_3 nanofluids turbulent flow was numerically investigated in a horizontal circular tube by Hejazian et al. [9]. They concluded that convective heat transfer coefficient increases with an increased Reynolds Numbers and volume fraction. Furthermore, these studies were widely investigated using nanofluids in the vertical tubes. [10] to [12].

He et al. [13] examined experimental heat transfer and flow behaviour in a vertical tube and concluded that by increasing the Reynolds Numbers, convective heat transfer coefficient and the flow pressure drop increase. Saberi et al. [14] investigated the numerically forced convective heat transfer of laminar flow with nanofluids under wall uniform heat flux in a vertical circular tube. They found that the convective heat transfer coefficient and the Nusselt number increase with increased Reynolds Numbers.

The inclined tubes also were selected for the studies [15] and [16]. Solar collectors are the most important devices which use of the inclined tubes to investigate heat transfer by using nanofluids is studied in them [17]. Numerical study of the mixed convective heat transfer water/ Al_2O_3 nanofluids laminar flow is conducted in the horizontal and inclined tubes by Akbari et al. [18]. They indicated that by increasing the inclination of the tube, surface friction coefficient continuously increases, but convective heat transfer coefficient has maximum value at an angle of 45° . Cimpean and Pop [19] investigated mixed convective heat transfer of laminar flow in an inclined channel and concluded that use of nanofluids increases heat transfer. Allahyari et al. [20] studied numerically mixed convective heat transfer of water/ Al_2O_3 nanofluids laminar flow with the wall non-uniform heat flux in an inclined circular tube; they concluded

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that convective heat transfer coefficient increases with enhancing nanoparticles volume fraction, but it decreases with increasing the tube angle from the horizontal surface. Mansour et al. [21] examined experimentally mixed convective heat transfer of water/Al₂O₃ nanofluids laminar flow in an inclined tube. They observed that by increasing nanoparticles volume fraction and the Reynolds number, the Nusselt number decreases. On the other hand, the Nusselt number increases with increasing the Grashof number. Investigating pressure drop of nanofluids laminar flow under the wall uniform heat flux studied experimentally in an inclined tube by Pirhayati et al. [22]. They made a conclusion that pressure drop increases with increasing volume fraction of nanoparticles, but increasing the inclination of the tube from the horizon from 0 degrees to 30 degrees for Reynolds number less than 170, reduces the pressure drop. Derakhshan and Akhavan-Behabadi [23] used fin and flat inclined tubes to evaluate the flow characteristic, pressure drop, and friction coefficient by using MWCNT– oil nanofluid. They observed that by increasing the inclination of the tube from 0 degrees to 90 degrees, the pressure drop and friction coefficient increase. Also, pressure drop in the fin tubes is more than the flat tubes. Maré, et al. [24] also analyzed experimentally mixed convective heat transfer of laminar flow in a circular inclined tube.

In this paper, the effect of Reynolds number on thermal and hydrodynamic parameters including convective heat transfer coefficient, Nusselt number, surface friction coefficient is investigated numerically in mixed convective heat transfer Al₂O₃/water nanofluids turbulent flow within an inclined copper tube under non-uniform heat flux of the upper wall and insulation of the lower wall by using two phase mixture model. According to the obtained numerical results, some equations are extracted to calculate the average Nusselt number and the wall surface friction coefficient in terms of Reynolds number changes and different inclinations of tube.

1 MATHEMATICAL MODELING

Turbulent mixed convection of a nanofluid consisting of water and Al₂O₃ in a horizontal circular tube with non-uniform heat flux on the upper wall and insulation in the lower wall has been considered. In order to discretize of governing equations the upstream difference scheme of second-order and finite volume method are used. Fig. 1 shows the considered geometrical configuration. The tube has a diameter of 0.01 m and a length of 1 m. Tube thickness to

diameter ratio of 0.1 is assumed. In this paper, the two phase mixture model is employed for the simulation. The nanofluid is a mixture of water and particles of Al₂O₃ and the size is uniform 32 nm.

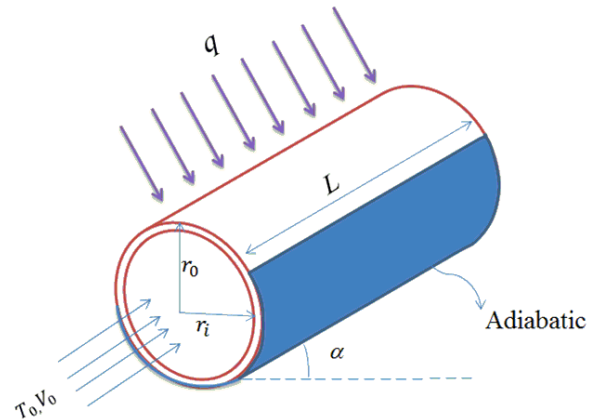


Fig. 1. Studied geometry (schematic of an inclined tube)

The conservation equations for steady state mixture model with assumption incompressible and Newtonian of flow are as follows [25]:

Continuity equation:

$$\nabla \cdot (\rho_m \mathbf{V}_m) = 0. \tag{1}$$

Conservation of momentum:

$$\begin{aligned} \nabla \cdot (\rho_m \mathbf{V}_m \mathbf{V}_m) = & -\nabla p_m + \nabla \cdot [\tau - \tau_t] - \\ & -\rho_{eff} \beta_{eff} (T - T_0) g + \\ & + \nabla \cdot \left(\sum_{k=1}^n \phi_k \rho_k \mathbf{V}_{dr,k} \mathbf{V}_{dr,k} \right). \end{aligned} \tag{2}$$

Conservation of energy:

$$\nabla \cdot (\phi_k \mathbf{V}_k (\rho_k h_k + p)) = \nabla \cdot (\lambda_{eff} \nabla T - C_p \rho_m \overline{vt}). \tag{3}$$

Conservation of energy:

$$\nabla \cdot (\phi_p \rho_p \mathbf{V}_m) = -\nabla \cdot (\phi_p \rho_p \mathbf{V}_{dr,p}), \tag{4}$$

where \mathbf{V}_m and ρ_m are defined as:

$$\mathbf{V}_m = \frac{\sum_{k=1}^n \phi_k \rho_k \mathbf{V}_k}{\rho_{eff}}, \quad \rho_m = \sum_{k=1}^n \phi_k \rho_k, \tag{5}$$

In Eq. (2), $\mathbf{V}_{dr,k}$ is the drift velocity for the secondary phase k , i.e. the nanoparticles in the present study which is defined as:

$$\mathbf{V}_{dr,k} = \mathbf{V}_k - \mathbf{V}_m, \tag{6}$$

and in Eq. (2), τ and τ_t are the viscous shear stress and turbulent shear stress which are defined as:

$$\tau = \mu_m \nabla \mathbf{V}_m, \quad \tau_t = -\sum_{k=1}^n \phi_k \rho_k \overline{v_k v_k}, \quad (7)$$

where μ_m is defined as:

$$\mu_m = \sum_{k=1}^n \phi_k \mu_k. \quad (8)$$

\mathbf{V}_{pf} is the slip velocity or relative velocity that defines as the velocity of a secondary phase (p) relative to the velocity of the primary phase (f).

$$\mathbf{V}_{pf} = \mathbf{V}_p - \mathbf{V}_f. \quad (9)$$

The drift velocity is related to the relative velocity which is defined as:

$$\mathbf{V}_{dr,k} = \mathbf{V}_{pf} - \sum_{k=1}^n \frac{\phi_k \rho_k}{\rho_m} \mathbf{V}_{fk}. \quad (10)$$

The relative velocity is determined from Eq. (9) proposed by Manninen et al. [26]:

$$\mathbf{V}_{pf} = \frac{\rho_p d_p^2}{18 \mu_f f_{drag}} \frac{(\rho_p - \rho_m)}{\rho_p} \mathbf{a}. \quad (11)$$

In this equation the drag function, f_{drag} is calculated by Schiller and Naumann [27]:

$$f_{drag} = \begin{cases} 1 + 0.15 Re_p^{0.687}, & Re_p \leq 1000 \\ 0.0183 Re_p, & Re_p \geq 1000 \end{cases}. \quad (12)$$

The acceleration (\mathbf{a}) in Eq. (11) is:

$$\mathbf{a} = \mathbf{g} - (\mathbf{V}_m \cdot \nabla) \mathbf{V}_m. \quad (13)$$

2 TURBULENCE MODELING

Turbulence is modeled with the Launder and Spalding [28] $k-\varepsilon$ turbulence model for the mixture. It is expressed by Eqs. (14) to (16):

$$\nabla \cdot (\rho_m \mathbf{V}_m k) = \nabla \cdot \left(\frac{\mu_{t,m}}{\sigma_k} \nabla k \right) + G_{k,m} - \rho_m \varepsilon, \quad (14)$$

$$\nabla \cdot (\rho_m \mathbf{V}_m \varepsilon) = \nabla \cdot \left(\frac{\mu_{t,m}}{\sigma_\varepsilon} \nabla \varepsilon \right) + \frac{\varepsilon}{k} (c_1 G_{k,m} - c_2 \rho_m \varepsilon), \quad (15)$$

where:

$$\mu_{t,m} = \rho_m c_\mu \frac{k^2}{\varepsilon}, \quad G_{k,m} = \mu_{t,m} (\nabla V_m + (\nabla V_m)^T), \\ c_1 = 1.44, c_2 = 1.92, c_\mu = .09, \sigma_k = 1, \sigma_\varepsilon = 1.3, \quad (16)$$

where c_1 and c_2 are constants.

3 BOUNDARY CONDITION

The boundary conditions are expressed as follows:

- At inlet of tube ($Z = 0$):

$$V_z = V_0, \quad V_\theta = V_r = 0, \quad T = T_0, \quad I = I_0. \quad (17)$$

Turbulent intensity calculated based on the formula [29]:

$$I_0 = 0.16 (Re)^{\frac{-1}{8}}. \quad (18)$$

- At the tube wall ($r = r_0$):

$$0 \leq \theta \leq \pi: \quad -\lambda_s \frac{\partial T_s}{\partial r} = q_w, \quad (19)$$

$$\pi \leq \theta \leq 2\pi: \quad -\lambda_s \frac{\partial T_s}{\partial r} = 0. \quad (20)$$

- At the solid/fluid interface: ($r = r_i$):

$$T_w = T_{nf}, \quad \lambda_s \frac{\partial T_w}{\partial r} = \lambda_{eff} \frac{\partial T_{nf}}{\partial r}, \quad V_z = V_r = V_\theta = 0. \quad (21)$$

- At the tube outlet:

The diffusion fluxes are set to zero at the exit for all dependent variables and an overall mass balance correction is obeyed.

4 NANOFUID THERMO-PHISICAL PROPERTIES

The physical properties are:

Effective density:

The nanofluid density is given by [30]:

$$\rho_m = (1 - \phi) \rho_f + \phi \rho_p, \quad (22)$$

where the volumetric concentration is given by:

$$\phi = \frac{\rho_f \phi_m}{\rho_f \phi_m + \rho_p (1 - \phi_m)}, \quad (23)$$

and where ϕ_m is the mass fraction.

An accurate equation is used for calculating the effective heat capacitance:

$$(C_p)_{eff} = \left[(1 - \phi) (\rho C_p)_f + \phi (\rho C_p)_p \right] / \rho_m. \quad (24)$$

The thermal conductivity of the nanofluid is calculated from Chon et al. [31] correlation, which considers the Brownian motion and mean diameter of the nanoparticles.

$$\lambda_{eff} / \lambda_f = 1 + 64.7 \times \phi^{0.746} \times (d_f / d_p)^{0.369} \times (\lambda_p / \lambda_f)^{0.746} \times Pr^{0.9955} \times Re^{1.2321}, \quad (25)$$

$$\frac{\lambda_{eff}}{\lambda_f} = 1 + 64.7 \times \phi^{0.746} \times \left(\frac{d_f}{d_p}\right)^{0.369} \times \left(\frac{\lambda_p}{\lambda_f}\right)^{0.746} \times Pr^{0.9955} \times Re^{1.2321}, \quad (25)$$

where Pr and Re in Eq. (25) are defined as:

$$Pr = \frac{\mu_f}{\rho_f \alpha_f}, \quad Re = \frac{\rho_f B_c T}{3\pi \mu^2 l_{bf}}, \quad \mu = A \times 10^{\frac{B}{T-C}},$$

$$C = 140, \quad B = 247, \quad A = 2.414e^{-5}. \quad (26)$$

l_{bf} is the mean free path of water and B_c is Boltzman constant ($B_c = 1.3807 \times 10^{-23}$ J/K).

Effective viscosity is calculated by the following equation proposed by Masoumi et al. [32] that considers the effects of volume fraction, density, and average diameter of nanoparticles and physical properties of the base fluid:

$$\mu_{eff} = \mu_f + \frac{\rho_p V_B d_p^2}{72C\delta},$$

$$V_B = \frac{1}{d_p} \sqrt{\frac{18K_b T}{\pi \rho_p d_p}}, \quad \delta = \sqrt[3]{\frac{\pi}{6\phi}} d_p, \quad (27)$$

$$C = \mu_f^{-1} \left[(c_1 d_p + c_2) \phi + (c_3 d_p + c_4) \right], \quad (28)$$

where c_1, c_2, c_3 and c_4 are:

$$c_1 = -0.000001133, \quad c_2 = -0.000002721,$$

$$c_3 = -0.00000009, \quad c_4 = -0.000000393.$$

Thermal expansion coefficient proposed by Khanafer et al. [33]:

$$\beta_{eff} = \beta_p / (1 + (1 - \phi) \rho_f / \phi \rho_p) \beta_f + 1 / (1 + \phi \rho_p / (1 - \phi) \rho_f). \quad (29)$$

5 NUMERICAL METHOD AND VALIDATION

In this work, the fluid enters the tube with a constant inlet temperature T_0 of 293 K and with uniform axial velocity of V_0 . The Reynolds number for simulation and selection grid of 5000 is assumed. This set of coupled nonlinear differential equations is discretized with the control volume technique. For the convective and diffusive terms the second order upwind method is used while the SIMPLEC procedure is introduced for the velocity–pressure coupling. A structured non-uniform grid distribution has been used to discretize the computation domain. It is finer near the tube inlet and near the wall where the velocity and temperature

gradients are large. Several different grid distributions have been tested to ensure that the calculated results are grid independent.

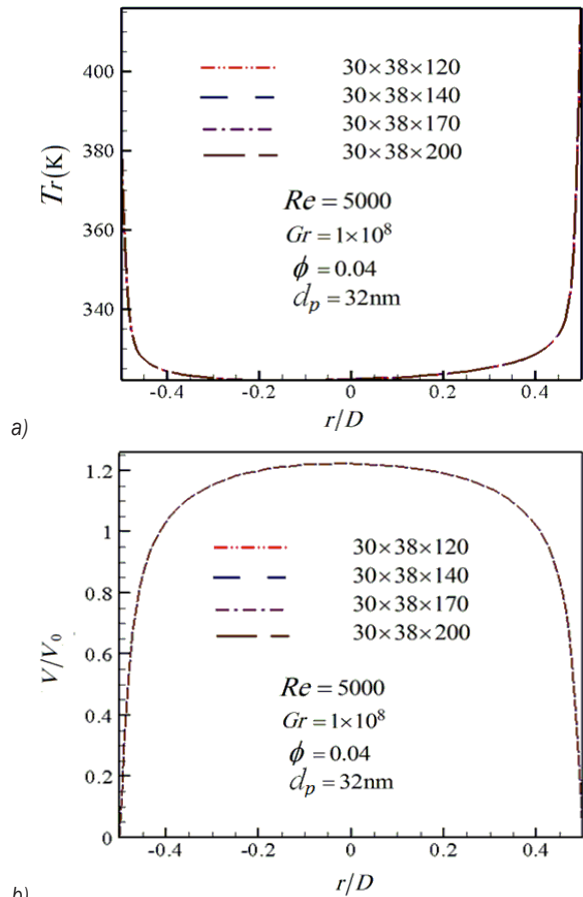


Fig. 2. Grid independence test: a) fully developed temperature, b) centerline axial velocity

The selected grid for the present calculations consisted of 170, 30 and 38 nodes, respectively, in the axial, radial and circumferential directions.

As shown in Fig. 2 increasing the grid numbers do not significantly change the velocity and temperature of the nanofluid. Other axial and radial profiles have also been verified to be sure the results are grid independent.

In order to demonstrate the validity and also precision of the model and numerical procedure, comparisons with the available experimental and numerical simulation have been done. As it is shown in Fig. 3, good agreements between the results are observed.

Fig. 3a shows the comparison of the calculated results with the results obtained by Gnielinski and

Sruher [34] and experimental results obtained by Wusiman et al. [35].

Another comparison has also been performed with the experimental results obtained by Torii [36]. (See Fig. 3b).

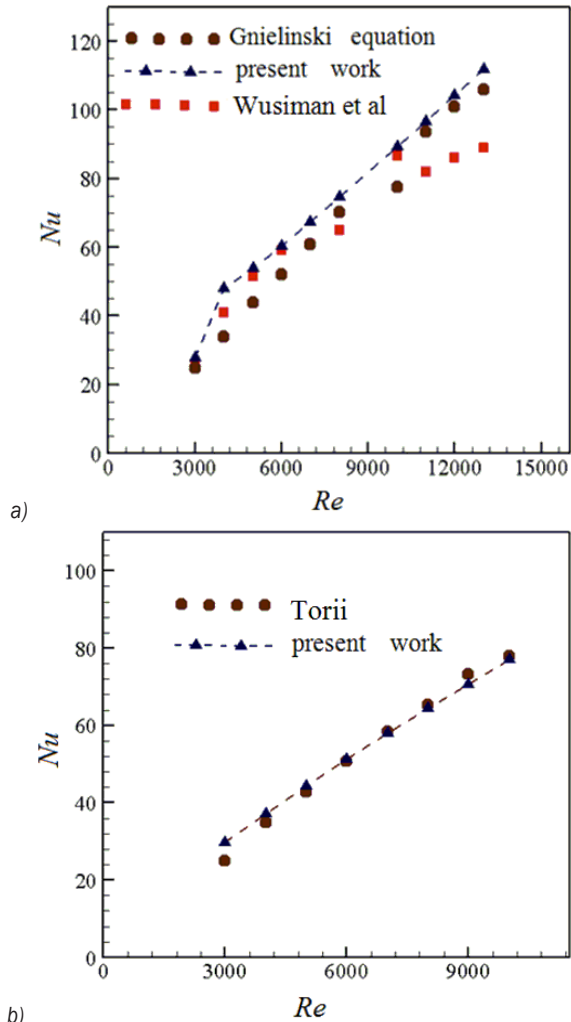


Fig. 3. Comparison of the axial evolution of Nu in a horizontal tube with the results obtained by a) Gnielinski and Sruher [34] and Wusiman et al. [35]; and b) Torii [36]

6 RESULTS

One important factor in the study of mixed convective heat transfer of the turbulent flow is to investigate the Reynolds number changes and its effect on thermal and hydrodynamic parameters. The Reynolds number, the volume fraction of nanoparticles and Grashof number are considered 4000 to 6000, 4 %, $Gr = 1 \times 10^8$ respectively. In this study, the inclination of the tube from horizon is considered 45 degrees

and flow of Aluminum oxide/water nanofluids is investigated. Considering that the Reynolds number is the ratio of inertial forces to viscosity forces, with constant volume fraction of the nanoparticles and thus constant viscosity forces, increase or decrease of the Reynolds number will increase or decrease the inertial forces. On the other hand, the Richardson number was defined as the ratio of the Grashof number to the square of Reynolds number in reference [20] and [38]. According to the reference [37], if the above ratio is $(Gr/Re^2 \ll 1)$, there will be forced convection heat transfer and we can neglect the effect of natural convection. If, $(Gr/Re^2 \gg 1)$, we will have natural convection heat transfer and can neglect the effect of forced convection. Regarding this subject, the references [20], [25] and [38] deal with the study of mixed convection heat transfer. Reference [38], shows the mixed convection heat transfer of nanofluid in laminar flow at Richardson numbers of ($Ri = 0.33, 1.66$ and 5) in a horizontal tube and reference [20], studied this matter in an inclined tube. Reference [25], also studied the mixed convection heat transfer of nanofluid of turbulent flow in a curved horizontal tube at similar Richardson numbers. As can be seen in references [20], [25] and [38], we will have mixed convection heat transfer at Richardson number ($Ri = 4$) that is assumed in the present paper. It means that we will have both the effects of buoyancy forces and inertia forces.

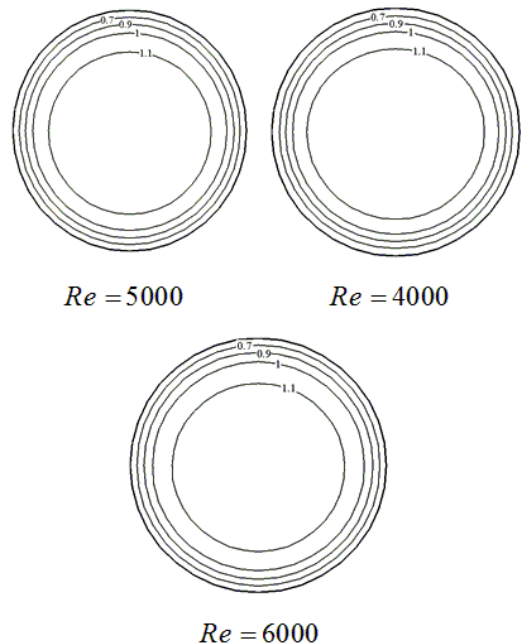


Fig. 4. Dimensionless axial velocity contours in the radial direction for different Reynolds numbers of $Z/D = 94, \phi = 0.04$ and $\alpha = 45$

Fig. 4 indicates dimensionless axial velocity contours for Grashof number $Gr = 1 \times 10^8$ at 4 % volume fraction in different Reynolds numbers and an angle of 45 degrees from horizon.

As figure shows, dimensionless axial velocity contours become longer in the vertical direction with increase of the Reynolds number and it will not have any movement to the up or down of the wall.

Fig. 5 shows dimensionless axial velocity profile in an inclined tube at an angle of 45 degrees from horizon at different Reynolds numbers. As can be seen, in this case velocity profile becomes more uniform with increasing the Reynolds number. Fig. 6 indicates dimensionless axial velocity profile on the tube centerline in an inclined tube at an angle of 45 degrees from horizon at different Reynolds numbers. It is shown in this figure that flow rate is reached to a maximum value after the tube inlet and then is developed. The reason for this is that after the tube inlet, the growth of the tube boundary layer causes contraction and conducts flow towards the tube centerline, thus increases the velocity on the tube centerline. By increasing the Reynolds number, the velocity maximum point inclines down, since by increasing the Reynolds number, the axial momentum and turbulence production in the flow direction increase.

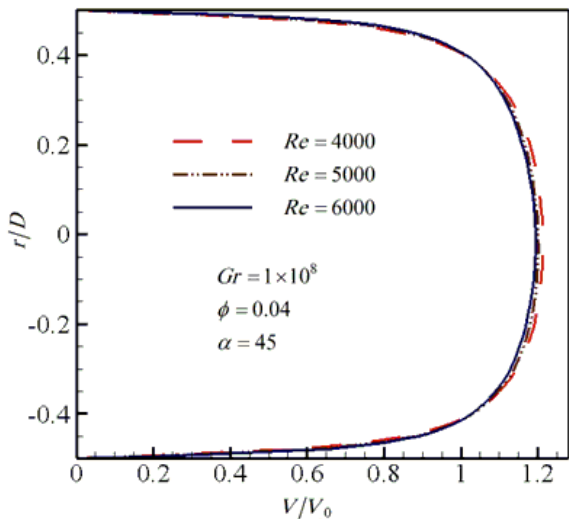


Fig. 5. Dimensionless axial velocity profile in the radial direction for different Reynolds numbers of $Z/D = 94$

The dimensionless axial velocity maximum and the amount of development reduce with increase of Reynolds number and the most important reason for this process is that the velocity profile become more uniform with the increase of Reynolds number.

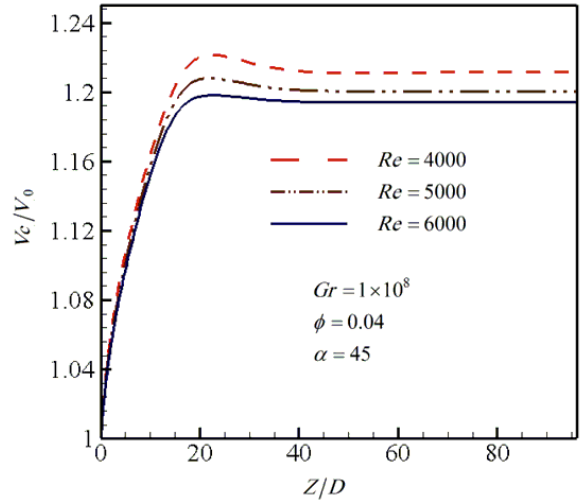


Fig. 6. Dimensionless axial velocity profile in the tube centerline for different Reynolds numbers

Fig. 7 displays dimensionless temperature contours on $Z/D = 94$ of an inclined tube with an angle of 45 degrees from horizon, constant Grashof number $Gr = 1 \times 10^8$, and 4 % volume fraction at different Reynolds numbers. As can be seen in the figure, dimensionless temperature decreases with the increase of the Reynolds number. At the end of the tube at high Reynolds, fluid has enough time to get the heat. So the temperature contours are asymmetric.

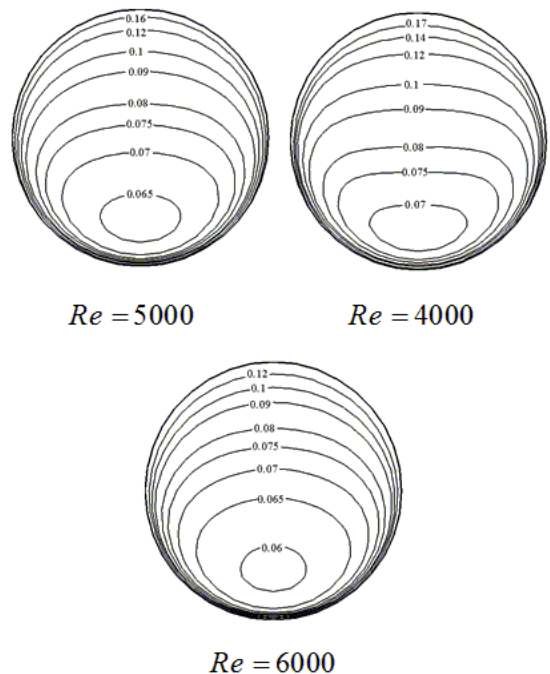


Fig. 7. Dimensionless temperature contours for different Reynolds numbers of $Z/D = 94$, $\phi = 0.04$, $Gr = 1 \times 10^8$ and $\alpha = 45$

Fig. 8 shows the turbulent kinetic energy profile at $Z/D = 94$ of an inclined tube with an angle of 45 degrees from horizon at Grashof number $Gr = 1 \times 10^8$, and different Reynolds numbers. In this figure, the turbulent kinetic energy increases with increase of the Reynolds number and its main reason will be increase of velocity and turbulences. Fig. 9 indicates changes of convective heat transfer coefficient in the tube dimensionless length within an inclined tube at different Reynolds numbers. At the beginning of the tube after the inlet, the convective heat transfer coefficient is very high due to the proximity of the wall temperature and the fluid bulk temperature. This coefficient reaches to the minimum value with distance from the inlet and there is maximum temperature difference between the wall temperature and the fluid bulk temperature in this area. Then, it remains constant due to the same temperature difference in the developed area. As observed in this figure, convective heat transfer coefficient increases with the increase of Reynolds number and its main reason is the increase of turbulent kinetic energy and turbulences.

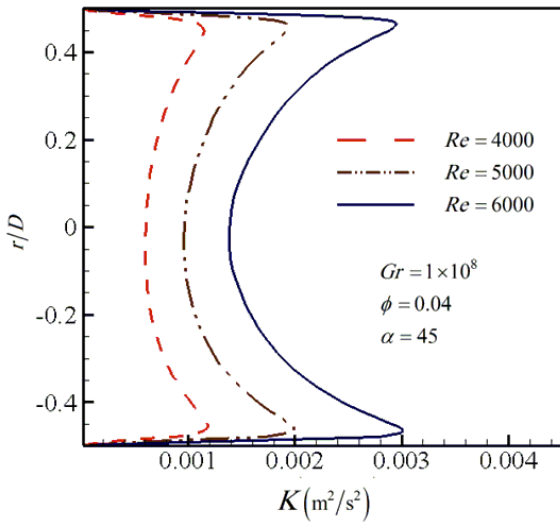


Fig. 8. Turbulent kinetic energy profiles in the radial direction for different Reynolds numbers of $Z/D = 94$

Fig. 10 displays the shear stress changes in the dimensionless length of an inclined tube with Grashof number $Gr = 1 \times 10^8$, and solid to liquid volume ratio of 4 % at different Reynolds numbers. By increasing Reynolds number in a constant volume fraction, the flow rate increases resulting in increased velocity gradient. With increase of the velocity gradient and constant viscosity, the shear stress increases. Fig. 11 shows changes of surface friction coefficient in the

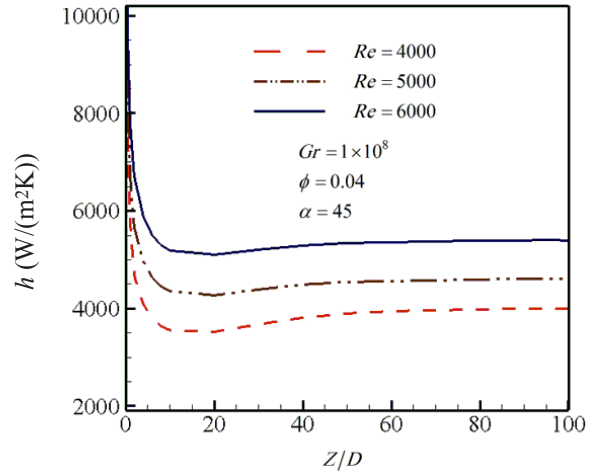


Fig. 9. Changes of convective heat transfer coefficient for different Reynolds numbers in the tube dimensionless length

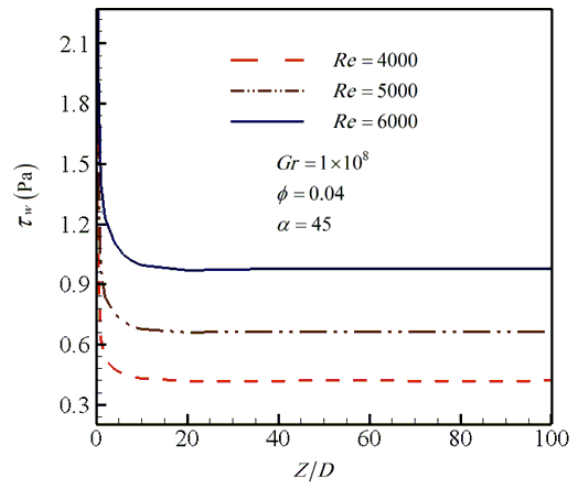


Fig. 10. Changes of shear stress in the dimensionless length of the tube for different Reynolds numbers

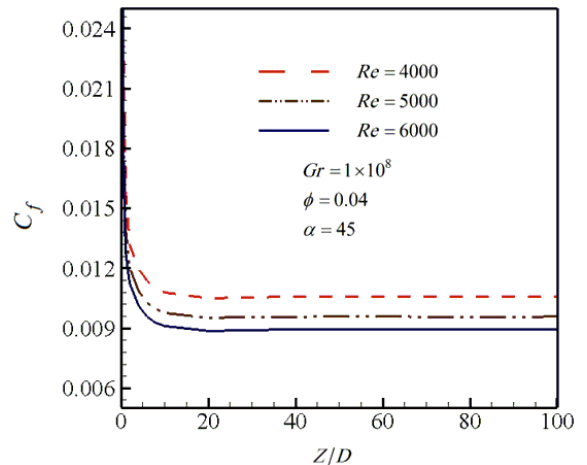


Fig. 11. Changes of surface friction coefficient in dimensionless length of the tube for different Reynolds numbers

tube dimensionless length within a horizontal inclined tube with Grashof number $Gr = 1 \times 10^8$, and solid to liquid volume ratio of 4 % at different Reynolds numbers. By increasing the Reynolds number, the surface friction coefficient of the tube decreases; this is because of interactions between shear stress and flow rate changes with increase of the Reynolds number.

Fig. 12 shows changes of convection heat transfer coefficient in dimensionless length of the tube at Grashof number $Gr = 1 \times 10^8$, Reynolds number $Re = 5000$, and with an angle of 45 degrees from horizon in different volume fraction of solid-liquid particles. As can be seen in this figure, by increasing volume fraction of the nanoparticles in an inclined tube, the convection heat transfer coefficient increases; the main reason is the fluid's thermo-physical characteristics improving with increase of nanoparticles volume fraction.

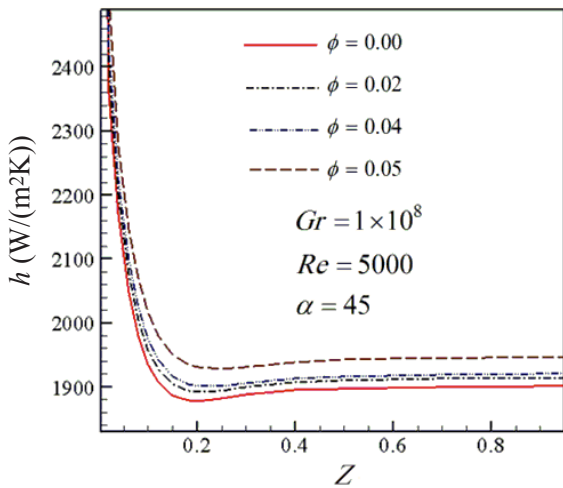


Fig. 12. Changes of convective heat transfer coefficient in dimensionless length of the tube for different volume fraction

7 EXTRACTED EQUATIONS FROM THIS STUDY

The behavior of nanofluids heat transfer depends on various parameters such as thermal conductivity, convective heat transfer coefficient, viscosity, heat capacity, angle of the tube from horizon, and volume fraction of nanoparticles. Considering investigation of the hydrodynamic and thermal behavior of nanofluids in an inclined tube, the following equations are obtained to calculate average Nusselt number and surface friction coefficient of the wall.

The following equations are for Nusselt number and surface friction coefficient in an inclined tube

which is a function of the Reynolds number and angle of the tube from the horizon surface. In the volume fraction $\phi = 0.04$ for the developed area, it obtains:

$$Nu_{av} = 0.115Re^{0.801}(34.408 + \alpha)^{-0.189}, \quad (30)$$

$$C_f = 0.31Re^{-0.391}(0.684 + \alpha)^{0.011}. \quad (31)$$

Fig. 13 displays changes of the average Nusselt number in terms of the Reynolds number in different angles within an inclined tube. As observed, the Nusselt number increases with increase of the Reynolds number. On the other hand, by increasing angle of the tube from horizon, the Nusselt number decreases in a certain Reynolds number. By comparing the obtained values from the Eq. (30) and numerical

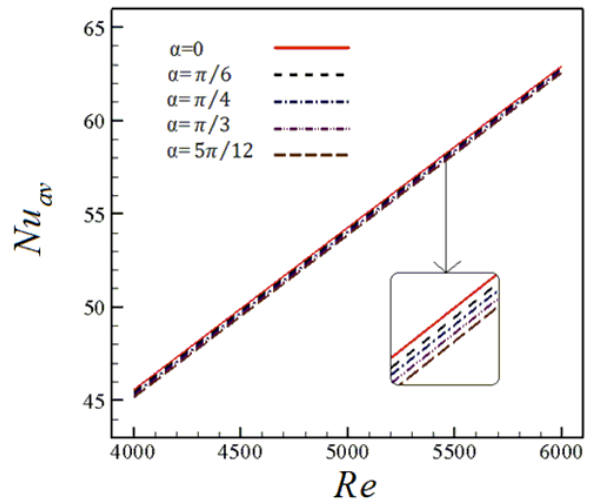


Fig. 13. Changes of average Nusselt number in terms of Reynolds number for different inclinations of tube

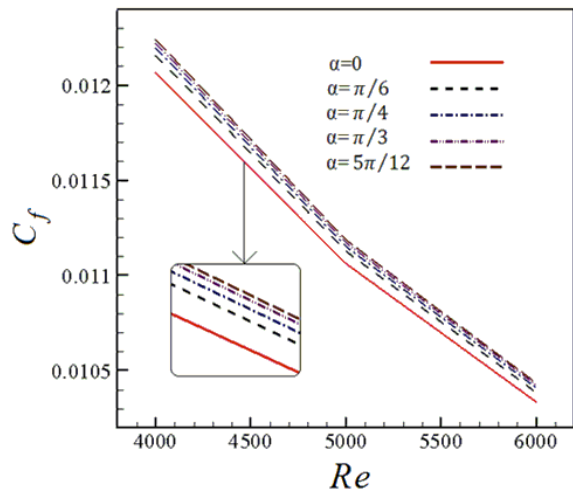


Fig. 14. Changes of surface friction coefficient in terms of Reynolds number for different inclinations of tube

data of the thesis, the correlation coefficient is equal to $R^2 = 0.9998$ for the Eq. (30).

Fig. 14 indicates changes of surface friction coefficient in terms of the Reynolds number in different angles within an inclined tube. As can be seen, by increasing the Reynolds number, the surface friction coefficient decreases. On the other hand, by increasing angle of the tube from horizon, the surface friction coefficient increases in a certain Reynolds number. By comparing the obtained values from the Eq. (31) and numerical data of the thesis, the correlation coefficient is equal to $R^2 = 0.9997$ for the Eq. (31).

8 CONCLUSION

In this paper, the effect of Reynolds number on thermal and hydrodynamic characteristics of the nanofluids turbulent flow mixed convective heat transfer within an inclined tube is numerically studied with non-uniform heat flux on the upper wall of the tube and insulation in the lower wall by using two phase mixture model. The results indicated that dimensionless axial velocity becomes more uniform with increase of the Reynolds number in a certain Grashof number and constant volume fraction. By increasing the Reynolds number, the axial momentum increases and turbulence produces in the flow direction. Dimensionless axial velocity maximum and the amount of development decreases with increase of the Reynolds number and the most important reason of this process is that the velocity profile becomes more uniform with increase of the Reynolds number. By increasing the Reynolds number, the turbulent kinetic energy increases and this is because of increase of velocity and thus the turbulences in the fluid. By increasing Reynolds number, the convective heat transfer coefficient and shear stress increase but the surface friction coefficient decreases.

9 NOMENCLATURES

a	acceleration [ms^{-2}]
C_f	average skin friction coefficient
C_p	specific heat of the fluid [$\text{Jkg}^{-1}\text{K}^{-1}$]
d_f	molecular diameter of base fluid [nm]
d_p	nanoparticle diameter [nm]
D	tube diameter [m]
g	gravity acceleration [ms^{-2}]
Gr	Grashof number
h	average convective heat transfer coefficient [$\text{Wm}^{-2}\text{K}^{-1}$]
K	turbulent kinetic energy [m^2s^{-2}]

L	channel length [m]
n	number of phase
p	pressure [Pa]
q	average wall heat flux [Wm^{-2}]
r	radial coordinate [m]
Re	Reynolds number
t	fluctuating temperature [K]
T	temperature [K]
V	velocity [ms^{-1}]
Z	axial coordinate [m]

Greek letters

α	Thermal diffusivity and inclination of tube [Wm^{-2}]
β	Volumetric expansion coefficient [K^{-1}]
ε	Dissipation of turbulent kinetic energy [m^2s^{-1}]
θ	Angular coordinate
ϕ	particle volume concentration
λ	thermal conductivity of the fluid [$\text{Wm}^{-1}\text{K}^{-1}$]
μ	fluid dynamic viscosity [$\text{Kgm}^{-1}\text{s}^{-1}$]
ν	kinematic viscosity [m^2s^{-1}]
ρ	fluid density [Kgm^{-3}]
τ	shear stress [Pa]

Subscript

b	bulk value
dr	drift
eff	effective
f	primary phase
k	k^{th} phase
m	mixture
nf	nanofluid
p	particle, secondary phase
s	solid
t	turbulent
w	wall
0	inlet condition

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