

**ON THE ESTIMATION OF PI INDEX OF POLYACENES<sup>#</sup>****Padmakar V. Khadikar\* and Sneha Karmarkar***Research Division, Laxmi Fumigation and Pest Control, Pvt. Ltd.,  
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<sup>#</sup>This paper is dedicated to Professor Ivan Gutman, teacher, inspirer, friend, and proprietor of graph theory and topology.

*Received 18-03-2002***Abstract**

General formulae are obtained for the PI (Padmakar-Ivan) index of polyacenes. The PI is a newly proposed molecular-graph-distance-based structural descriptor. By means of this result it was possible, for the first time, to examine relative correlation potential of Wiener (W)-, Szeged (Sz)- first-order connectivity ( ${}^1\chi$ ), and PI indices in developing Quantitative Structure-Property Relationships (QSPRs) of polyacenes in that hydrophobicity of polyacenes is used as the correlating property.

**Introduction**

A topological index is a numerical quantity derived in an unambiguous manner from the structural graph of a molecule.<sup>1–5</sup> It is a number extracted by a well defined algorithm from a graphical representation of a molecule. There is good reason to believe that often our difficulties in attributing a meaning to this number lie under deeper chemical theories and higher level languages and not from esoteric approaches to its definition. These indices are graph invariants which usually reflect molecular size, shape, branching, and heterogeneity.<sup>4,5</sup>

Wiener originally defined<sup>6</sup> his index (*W*) on trees and studied its use for correlations of physicochemical properties of alkanes, alcohols, amines, and their analogous compounds.<sup>7,8</sup>

The original definition<sup>6</sup> of Wiener index (*W*) was given in terms of edge weights. In an arbitrary tree, every edge is a bridge, that is, after deletion of the edge; the graph is no more connected. The weight of an edge is taken to be the product of the number of vertices in the two connected components. This number also equals the

number of all shortest paths in the tree, which go through the edge. Therefore, the usual generalization to the Wiener Index ( $W$ ) on arbitrary graphs is defined to be the same of all distances in a graph.

Another natural generalization was previously put forward by Gutman<sup>9,10</sup> and called the Szeged index, abbreviated as  $Sz$ . Now, the weights of edges are taken to be the product of the numbers of vertices closed to the two ends of the edge. For reasons to introduce Szeged index, and for its basic properties, uses see reference.<sup>11–60</sup>

Wiener index ( $W$ ) is the first, oldest, and widely used topological index. Even to day it is widely used in chemistry.<sup>11–60</sup> The Szeged index ( $Sz$ ) is considered as a modification of Wiener index ( $W$ ) to cyclic graphs.<sup>11</sup> For trees (acyclic graphs) Wiener and Szeged indices coincide. Comparatively little is known on the applications of Szeged index in chemistry.

For the reason of the coincidence of Wiener and Szeged indices in case of trees (acyclic graphs), we have very recently introduced another Szeged / Wiener-like topological index and named it Padmakar-Ivan index, and abbreviated as  $PI$ .<sup>61–66</sup> Unlike Szeged index ( $Sz$ ),  $PI$  index is different for trees as well as for cyclic graphs, and not much is known about the applicability of  $PI$  index in chemistry.

In our earlier publications<sup>61–66</sup> we have defined  $PI$  index and discussed some of its characteristics and applicability in developing quantitative structure-property-activity (QSPR/QSAR) relationships and observed that  $PI$  index is quite useful in this respect. In addition, we have made comparative study of  $PI$  index with several other topological indices including  $W$ ,  $Sz$ , and connectivity indices ( ${}^m\chi^R$ ) and observed that  $PI$  index in some cases gives better results.<sup>40,67</sup> There we have used physicochemical property and biological activity of  $n$ -alkanes, cycloalkanes, alcohols, polychlorinated biphenyls, and monosubstituted nitrobenzene. However, we have not included benzenoid hydrocarbons in such studies. The present communication is, therefore, an extension of such study to benzenoid systems, in that we discuss the methods for the calculation of  $PI$  index for polyacenes. The other objective of our present study is to compare  $W$ ,  $Sz$ , and  $PI$  indices of polyacenes. Finally, we will make an attempt to use  $PI$  index for modeling

hydrophobicity ( $\log P$ ) of polyacenes, thus attempting QSPR/QSAR for this interesting class of benzenoid hydrocarbons. The results as discussed below show that we are quite successful in this respect.

## Results and Discussion

### Linear Polyacenes

Linear polyacenes (Figure 1) are the most thoroughly investigated homologous series of conjugated molecules (benzenoid systems). A plethora of theoretical work exists devoted to these systems.<sup>68–80</sup> However, nothing is known regarding different methods of calculating  $PI$  index of polyacenes and their applicability in QSPR/QSAR studies. For QSPR/ QSAR study we need methods for efficient calculations of  $PI$  index. Below we present such methods. However, we first repeat in brief, the general definition of  $PI$  index.

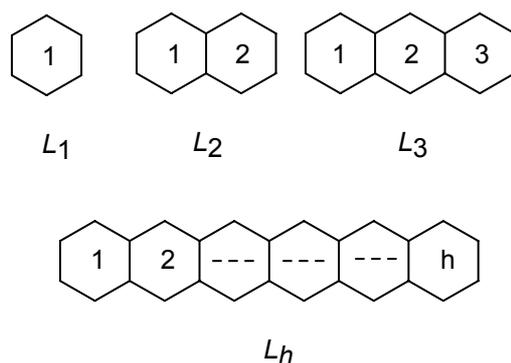


Fig. 1. Polyacene molecules

### Definition of $PI$ Index

Let  $G$  be a molecular graph, the vertex and edge sets of which are represented by  $V(G)$  and  $E(G)$  respectively. If  $e$  is an edge of  $G$ , connecting vertices  $u$  and  $v$  then we write  $e = uv$ . The number of vertices of  $G$  is denoted by  $|G|$ .

The distance between a pair of vertices  $u, w$  of  $G$  is denoted by  $d(u, w|G)$ .

We define for  $e = uv$ , two quantities  $\eta_{eu}(e|G)$  and  $\eta_{ev}(e|G)$ .  $\eta_{eu}(e|G)$  is the number of edges lying closer to the vertex  $u$  than the vertex  $v$ , and  $\eta_{ev}(e|G)$  is the number of edges lying closer to the vertex  $v$  than the vertex  $u$ . Edges equidistant from

both ends of the edge  $uv$  are not counted (taken into account), then the  $PI$  index is defined as:<sup>61–66</sup>

$$PI = \sum_e [ \eta_{eu}(e|G) + \eta_{ev}(e|G) ] \quad (1)$$

The summation goes over all the edges of  $G$ .

### The $PI$ Index of Polyacenes

As stated earlier, in order to be able to undertake studies on the applicability of  $PI$  index of polyacenes, we need method(s) of its efficient calculation. In the following sections we present such methods for the calculation of  $PI$  index of polyacenes for the first time.

It is well known that polyacenes are linearly para-annelated benzenoids, which possesses transitional symmetry (Figure 1). Chemistry of polyacenes is still very much of interest to synthetic chemists, environmental chemists, cancer research chemists, structural chemists, etc.<sup>73–80</sup> We believe that now  $PI$  index will be of better value for such diversified studies.

The hexagonal chain whose  $h$  hexagons are arranged in a linear manner is denoted by  $L_h$ ; the respective benzenoid hydrocarbons form the linear homologous series (benzene, naphthalene, anthracene, etc.) Note that the number of hexagons in the hexagonal chain  $C$  is denoted by  $h$ . Thus, we have  $C_1 = L_1$ ,  $C_2 = L_2$ ,  $C_3 = L_3$ , ....., and so on. The structure of polyacene ( $L_h$ ) is shown in Fig.1.

From the definition of  $PI$  index (equation 1) and from the molecular graph of polyacene molecules (Figures 2 and 3), we observed that for any edge like  $a_i b_i$ ,  $a_i b_{i+1}$ ,  $c_i d_i$ ,  $d_i c_{i+1}$ ,  $i = 1, 2, 3, \dots, n$ , we have:

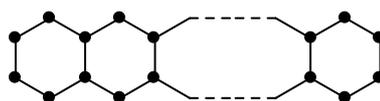
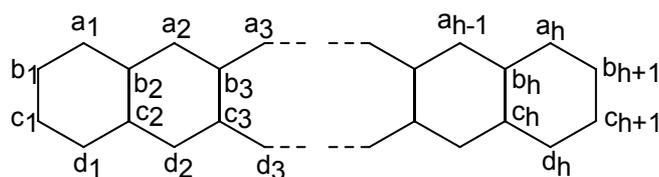


Fig. 2. Molecular graph ( $G_h$ ) of polyacenes



**Fig. 3.** Case of polyacenes used for the estimation of *PI* index

$$\eta_1(e) = |E_1| = 5_i - 3 \quad (2)$$

and  $\eta_2(e) = |E_2| = 5h - (5_i - 2) \quad (3)$

Thus giving,

$$\eta_1(e) + \eta_2(e) = |E_1| + |E_2| = 5h - 1 \quad (4)$$

Similarly, for any edge like  $b_i c_i$ ,  $i = 1, 2, 3, \dots, h+1$ , we have:

$$\eta_1(e) + \eta_2(e) = |E_1| + |E_2| = 4h \quad (5)$$

Hence, *PI* index of the polyacene will be given by:

$$PI(L_h) = 4h(5h - 1) + 4h(h + 1) = 24h^2 \quad (6)$$

Recall that  $L_h$  has  $2(2h + 1) = n$  vertices. In view of this  $PI(L_h)$  in terms of vertices  $n$  is given by the following expression:

$$PI(L_h) = 3/2(n-2)^2 \quad (7)$$

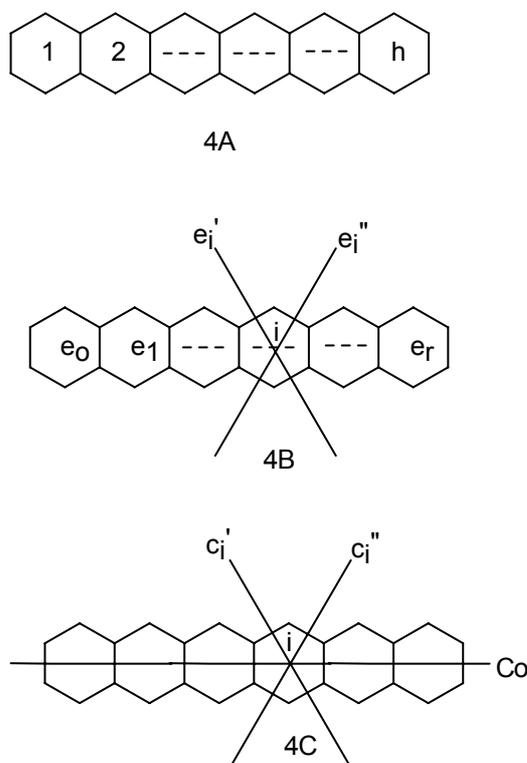
The *PI* indices so calculated for the first 20 polyacenes are given in Table 1.

#### ***A Case when Calculation of PI Index for Polyacene is Easy***

Now consider Figure 4B, in that edges  $e_0, e_1, e_2, e_3, \dots, e_r$  are called vertical edges of the polyacenes and are represented by  $V_E$ , while those denoted by  $e_i'$  and  $e_i''$  ( $i = 0, 1, 2, 3, \dots, n$ ) are called non-vertical edges ( $NV_E$ ) of polyacenes. The sum of the vertical and non-vertical edges is denoted by  $m$ , such that  $V_E + NV_E = m$ . The number of hexagons and edges in polyacenes are denoted by  $h$  and  $m$  respectively.

The lines crossing the vertical and non-vertical edges (Figure 4C) are called elementary cuts and play a distinguish role in the theory of benzenoid system.

The elementary cuts for the vertical edges ( $e_0, e_1, e_2, \dots, e_r$ ) is presented by  $C_0$ . The elementary cuts of non-vertical edge for the  $i^{\text{th}}$  hexagon is represented by  $C_i'$  and  $C_i''$  respectively in Figure 4C.



**Fig. 4.** Used for proposing alternative method of estimation  $PI$  index of polyacenes

The values of  $h$ ,  $n$ ,  $V_E$ ,  $NV_E$  and  $m$  for the first twenty members of the polyacene series are given in Table 1. The  $PI$  values estimated from Equation (1) are given in Table 2. The  $PI$  values calculated from equations (6) and (7) are also found to be the same.

Now, a critical examination of the calculation  $PI$  index using equation (1) indicates that in terms of  $V_E$ ,  $NV_E$  and  $m$  the estimation of  $PI$  index is still easy and consists of the following two terms:

- (1)  $(V_E) \cdot (NV_E)$ , and
- (2)  $(m-2) \cdot NV_E$

Thus giving:

$$PI = (V_E) \cdot (NV_E) + (m-2) NV_E \quad (8)$$

Say for example, for the polyacenes  $L_1$  (i.e., benzene,  $V_E = 2, NV_E = 4$ ). Therefore,  $m = V_E + NV_E = 6$ .

Therefore, equation (8) gives  $PI$  Index for  $L_1$  as:

$$PI(L_1) = (2 \times 4) + (6 - 2) 4 = 8 + 16 = 24 \quad (9)$$

which comes out to be the same when  $PI$  index for  $L_1$  is calculated from equations (1), (6) and (7).

**Table 1.** Calculated values of  $PI$  index for polyacenes using equation 1 and the  $\log P$  values of polyacene molecules.

S. No.	$L$	$n$	Names of abbreviated polyacenes	$PI$	$\log P$
1	1	6	$L_1$	24	2.202
2	2	10	$L_2$	96	3.396
3	3	14	$L_3$	216	4.590
4	4	18	$L_4$	384	5.784
5	5	22	$L_5$	600	6.978
6	6	26	$L_6$	864	8.172
7	7	30	$L_7$	1172	9.366
8	8	34	$L_8$	1536	10.560
9	9	38	$L_9$	1922	11.754
10	10	42	$L_{10}$	2400	12.948
11	11	46	$L_{11}$	2904	14.142
12	12	50	$L_{12}$	3456	15.336
13	13	54	$L_{13}$	4056	16.530
14	14	58	$L_{14}$	4704	17.724
15	15	62	$L_{15}$	5400	18.918
16	16	66	$L_{16}$	6144	20.112
17	17	70	$L_{17}$	6936	21.306
18	18	74	$L_{18}$	7776	22.500
19	19	78	$L_{19}$	8664	23.694
20	20	82	$L_{20}$	9600	24.880

**Table 2.** Data needed for alternative method for the calculation of PI index of polyacenes

Polyacenes	$L$	$n$	$NV_E$	$V_E$	$NV_E+V_E$	PI from eqs. 8, 13 & 14
$L_1$	1	6	4	2	6	24
$L_2$	2	10	8	3	11	96
$L_3$	3	14	12	4	16	216
$L_4$	4	18	16	5	21	384
$L_5$	5	22	20	6	26	600
$L_6$	6	26	24	7	31	864
$L_7$	7	30	28	8	36	1176
$L_8$	8	34	32	9	41	1536
$L_9$	9	38	36	10	46	1949
$L_{10}$	10	42	40	11	51	2400
$L_{11}$	11	46	42	12	56	2904
$L_{12}$	12	50	48	13	61	3456
$L_{13}$	13	54	52	14	66	4056
$L_{14}$	14	58	56	15	71	4704
$L_{15}$	15	62	60	16	76	5400
$L_{16}$	16	66	64	17	81	6144
$L_{17}$	17	70	68	18	86	6936
$L_{18}$	18	74	72	19	91	7776
$L_{19}$	19	78	76	20	96	8664
$L_{20}$	20	82	80	21	101	9600

Similarly, we can calculate  $PI$  indices for the set of 20 polyacene molecules from their respective values of  $V_E$ ,  $NE_V$  and again found to be the same as presented in Table 1 (Table 2).

#### ***A Case when Estimation of PI is Still Easier***

A perusal of Table 2 shows that:

$$V_E = h + 1 \quad (10)$$

and  $NV_E = 4h \quad (11)$

So that,

$$m = 4L + h + 1 = 5h + 1 \quad (12)$$

Substituting the values of  $V_E$ ,  $NE_V$ , and  $m$  in equation (8) we get the following:

$$\begin{aligned}
 PI &= (V_E) (NV_E) + (m - 2) NV_E & (13) \\
 &= 4h (h + 1) + \{ (5h + 1 - 2) 4h \} \\
 &= 4h (h + 1) + 4L (5h - 1) \\
 &= 4h \{ h + 1 + 5h - 1 \} \\
 &= 4h (6h) \\
 &= 24h^2 & (14)
 \end{aligned}$$

Thus, the estimation of  $PI$  index of polyacenes is made still easier by equation (13).

### **Comparison of $W$ , $Sz$ , and $PI$ Indices of Polyacenes**

It will be interesting to study relatedness among  $W$ ,  $Sz$ , and  $PI$  indices of polyacenes. Such a study will provide us a way to predict their relative correlation potential in developing QSPR/QSAR relationships.

As stated above the expression for estimating  $PI$  index (equation 6) is:

$$PI(L_h) = 24 h^2$$

The corresponding expressions for estimating  $W$  and  $Sz$  are as under:<sup>77,78</sup>

$$W(L_h) = 1/3 (16h^3 + 36h^2 + 26h + 3) \quad (15)$$

$$Sz(L_h) = 1/3 (44h^3 + 72h^2 + 43h + 3) \quad (16)$$

From the aforementioned equations (15) and (16) we observed that  $Sz$  index for linear polyacenes have a similar cubic polynomial dependence on molecular size as that of  $W$  index, but  $PI$  has not. Furthermore, the coefficient involved in these equations (15) and (16) are much higher than in the equation (6). In fact the coefficients of  $h$  terms are largest for equation (16). This indicates that the numerical value of  $Sz$  will be the largest among the three topological indices under present investigation. The order of the magnitudes of  $W$ ,  $Sz$ , and  $PI$  indices follow the following sequence:

$$Sz(L_h) > W(L_h) > PI(L_h) \quad (17)$$

The values of  $Sz$ ,  $W$  and  $PI$  indices for the first 20-polyacene molecules are presented in Table 3. The best account of the relatedness of  $W$ ,  $Sz$  and  $PI$  of polyacenes

could be made by subjecting the data in Table 3 to regression analysis. First step in such a study is to obtain correlation matrix. Such a matrix obtained in the present study is presented in Table 4. The regression analysis gives regression parameters as well as quality of relatedness.<sup>81–85</sup> The quality parameters are presented in Table 4.

**Table 3.**  $W$ ,  $Sz$ ,  $PI$  and  ${}^1\chi$  indices of polyacenes

Polyacenes	$W$	$Sz$	$PI$	${}^1\chi$
$L_1$	27	54	24	3.000
$L_2$	109	243	96	4.967
$L_3$	279	640	216	6.933
$L_4$	569	1381	384	8.899
$L_5$	1011	2506	600	10.866
$L_6$	1637	4119	864	12.832
$L_7$	2479	6308	1176	14.798
$L_8$	3569	9161	1536	16.765
$L_9$	4939	12766	1944	18.731
$L_{10}$	6621	17211	2400	20.697
$L_{11}$	86457	22584	2904	21.663
$L_{12}$	11049	28933	3456	24.630
$L_{13}$	13859	36466	4056	26.596
$L_{14}$	17109	45151	4704	28.562
$L_{15}$	20831	55116	5400	30.529
$L_{16}$	25057	66449	6144	32.495
$L_{17}$	29819	292230	6936	34.641
$L_{18}$	35149	93571	7770	36.428
$L_{19}$	41079	109536	8664	38.394
$L_{20}$	47641	127221	9600	40.360

**Table 4.** Correlation matrix for investigating relatedness among  $W$ ,  $Sz$ , and  $PI$  indices of polyacenes

	$W$	$Sz$	$PI$
$W$	1.0000		
$Sz$	0.9999	1.0000	
$PI$	0.9887	0.9885	1.0000

Proposed regression expressions:

$$PI(L_h) = 0.1672 (\pm 0.0053) W(L_h) + 1075.3313$$

$$PI(L_h) = 0.0625 (\pm 0.0020) Sz(L_h) + 1096.6398$$

Quality of aforementioned correlations:

Correlation	<i>Se</i>	<i>R</i>	<i>F</i>	<i>P</i>	<i>Q</i>
<i>PI</i> – <i>W</i>	724.1565	0.9887	1001.679	0.000E+00	0.0014
<i>PI</i> – <i>Sz</i>	731.8385	0.9885	980.280	0.000E+00	0.0014

A perusal of Table 4 shows that *W*, *Sz* and *PI* are highly linearly correlated; *Sz* correlates with *W* slightly more than *PI* index; while the correlation of *PI* index with *W* and *Sz* is similar. The corresponding relatedness of *PI* with *W* and *Sz* is given by the following regression expressions:

$$PI(L_h) = 0.1672 W(L_h) + 1075.3313 \quad (18)$$

and  $PI(L_h) = 0.0625 Sz(L_h) + 1096.6398 \quad (19)$

The corresponding qualities viz., standard error of estimation (*Se*), correlation coefficient (*R*), F-ratio, and probability values also indicates similar relatedness between *PI*-*W* and *PI*-*Sz* (Table 4).

It is worth recording that in addition to high relatedness, a particular index will be preferred over the other index in that fewer efforts are made for its estimation. Therefore, compared to both *W* and *Sz*, *PI* index is better as it is given by  $4h^2$  only. Thus, least efforts are required for its calculation.

From the aforementioned results and discussion we can conclude that correlation potential of *W*, *Sz*, and *PI* indices are similar. Also that, like *W* and *Sz*, *PI* index also takes care of size, shape and branching. The size-shape dependence of *W* and *Sz* is well established[86-88]. But, as discussed below we observe that *PI* index contains hither to unknown structural features, which dominates over size and shape. This makes *PI* index to give better results than *W* and *Sz* in some cases.<sup>61</sup>

### Modeling of Hydrophobicity of Polyacenes Using $W$ , $Sz$ , and $PI$ Indices

It is well established that hydrophobic interaction in biosystems can be modelled by  $\log P$  i.e. logarithm of partition coefficient ( $P$ ) between octanol-water or in some other suitable organic solvent / water partitioning systems.<sup>81–92</sup> Modeling of  $\log P$  with molecular descriptors (topological indices) has two-fold advantage, first  $\log P$  is considered as a physicochemical property and secondly it can also be used to represent physiological activity of organic compound acting as drugs.

The  $\log P$  values<sup>89–92</sup> for the first 20 polyacene molecules are presented in Table 5. In addition to  $W$ ,  $Sz$  and  $PI$  indices we have also chosen  ${}^1\chi$ -index<sup>67</sup> because it is most widely used topological index in QSPR and QSAR studies. That is now, we are considering relative ability of  $W$ ,  $Sz$ ,  $PI$ , and  ${}^1\chi$  indices for modeling, monitoring, estimating  $\log P$  of polyacenes. These  ${}^1\chi$  values are presented in Table 3.

**Table 5.** Correlation matrix for investigation relatedness among  $W$ ,  $Sz$ ,  $PI$ , and  ${}^1\chi$  and their correlation with  $\log P$  of polyacene molecule

	$\log P$	$W$	$Sz$	${}^1\chi$	$PI$
$\log P$	1.0000				
$W$	0.9264	1.0000			
$Sz$	0.9258	0.9999	1.0000		
${}^1\chi$	0.9999	0.9273	0.9267	1.0000	
$PI$	0.9707	0.9887	0.9885	0.9713	1.0000

Proposed regression expressions for modeling  $\log P$  of polyacene molecules using  $W$ ,  $Sz$ ,  ${}^1\chi$ , and  $PI$  indices.

$$\log P = 2.9087 \times 10^{-4} (\pm 2.4652 \times 10^{-5}) W + 9.171;$$

$$\log P = 1.088 \times 10^{-4} (\pm 9.2641 \times 10^{-6}) Sz + 9.211;$$

$$\log P = 0.6070 (\pm 1.7450 \times 10^{-3}) {}^1\chi + 0.1240;$$

$$\log P = 1.8027 \times 10^{-3} (\pm 9.3062 \times 10^{-5}) PI + 6.9680.$$

Quality of aforementioned correlations:

Correlating parameter	<i>Se</i>	<i>R</i>	<i>F</i>	<i>P</i>	<i>Q</i>
<i>W</i>	3.3800	0.9260	139.215	3.099 x 10 <sup>-11</sup>	0.2740
<i>Sz</i>	3.3940	0.9260	137.867	3.406 x 10 <sup>-11</sup>	0.2728
<sup>1</sup> $\chi$	0.1240	1.0000	120842.000	0.00E+0	8.0645
<i>PI</i>	2.1570	0.9710	375.224	0.000E+0	0.4502

We have first obtained correlation matrix for the parameters *W*, *Sz*, *PI*, <sup>1</sup> $\chi$  and  $\log P$  (Table 5). This correlation matrix indicates that compared to both *W* and *Sz*, *PI*-index is a better topological index for modeling  $\log P$  of polyacene molecules. However, <sup>1</sup> $\chi$  is the most appropriate index for this purpose. That is, correlation potential of *PI* index in modeling  $\log P$  is inferior to <sup>1</sup> $\chi$  but superior than *W* and *Sz*. Whether this is the case with other properties / activities is a problem for further investigation. Attempts in this direction are under way and the results will be published soon.

In order to obtain better insight into the problem of modeling  $\log P$  with *W*, *Sz*, *PI*, <sup>1</sup> $\chi$  we have subjected the data to regression analysis and obtained corresponding regression parameters i.e., the values of *Se*, *R*, *F*, *P* and *Q* (Table 5). Here, *Q* is the quality factor<sup>93,95</sup> obtained from the ratio of correlation coefficient (*R*), and standard error of estimation (*Se*) ( $Q = R/Se$ ). The advantage of using *Q* is that it takes accounts of *R* and *Se* simultaneously. The quality factor *Q* is directly proportional to *R* and inversely proportional to *Se*. Hence, larger the value of *R*, smaller the *Se*, higher will be *Q*, and the better will be the proposed correlation.

The data presented in Table 5 indicates that correlation potential of *W* and *Sz* in modeling  $\log P$  of polyacene molecules is similar. The *PI* index, is slightly more efficient than *W* and *Sz* for this purpose and that <sup>1</sup> $\chi$  is the most appropriate index among *W*, *Sz*, *PI* and <sup>1</sup> $\chi$  for modeling  $\log P$ . *Q*-values show that <sup>1</sup> $\chi$  is almost two-fold better index than *PI*, and that the relative potential of the topological indices in modeling  $\log P$  follow the following sequence.

$${}^1\chi(L_h) > PI(L_h) > W(L_h) \approx Sz(L_h) \quad (20)$$

Once again we state that shape-size dependence of  $W$  and  $Sz$  is well established. In spite of high collinearity among  $W$ ,  $Sz$ , and  $PI$ , the  $PI$  index is found better than both  $W$  and  $Sz$ . The  $Q$ -value of 0.4502 compared to  $\approx 0.2746$  or 0.2728 indicates that in addition to size and shape, the  $PI$  index contains some other hitherto unknown structural feature, which dominates over shape and size. As stated earlier the study in this direction is underway and results will be published soon.

In order to investigate probable unknown parameter(s) hidden in  $PI$  index we considered the polynomials for  $\log P = f(L)$  and  $\log P = f({}^1\chi)$ . From the data presented in Table 5 we have:

$$\log P = 1.8022 \times 10^{-3} (\pm 9.3062 \times 10^{-5}) PI + 6.9680 \quad (21)$$

and, 
$$\log P = 0.6070 (\pm 1.7450 \times 10^{-3}) {}^1\chi + 0.1240 \quad (22)$$

The first order connectivity index ( ${}^1\chi$ ) conveys more information about the number of atoms in a molecule. Therefore, according to equation (22) it is the atomic contribution, which accounts for the exhibition of  $\log P$ . Similarly, according to equation (21), the  $PI$  index is directly related to  $\log P$ . While the definition of  $PI$  index ( $= 24 h^2$ , equation 6) shows that  $PI$  is directly related to number of cycles ( $h$ ) present in the polyacene molecule. Hence, the unknown parameter hidden in  $PI$  index is the cyclicity. That is, in addition to first, shape, branching, the  $PI$  index also accounts for cyclicity, thus, hitherto unknown structural features contained in  $PI$  index is the cyclicity which dominates over shape and size.

### Conclusions

The aforementioned results and discussion lead us to the following conclusions:

- (1) The estimation of  $PI$  index for polyacene molecules is much simpler than the estimation of  $W$  and  $Sz$ ;
- (2) Both  $W$  and  $Sz$  are cubic polynomials while  $PI$  index is not;
- (3) Coefficient of  $h$  parameters in the corresponding expressions proposes the following order of magnitudes of  $W$ ,  $Sz$ , and  $PI$ .

$$Sz(L_h) > W(L_h) > PI(L_h);$$

- (4) High collinearity among  $W$ ,  $Sz$ , and  $PI$  indicates their similar correlation potential in proposing QSPR/QSAR models, and also their similar dependence on shape and size;
- (5) High quality of correlation of  $\log P$  with  $PI$ , compared to both  $W$  and  $Sz$ , indicates that in addition to size and shape, the  $PI$  index depends upon some hitherto unknown structural feature which dominates over shape and size.

### Experimental

For the calculation of  $PI$  index the molecular structures are transformed into their molecular graphs in that atoms (vertices) are depicted by dots and bonds (edges) by small lines.

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### Povzetek

Prikazane so splošne formule za PI (Padmakar-Ivan) indekse poliacenov. PI je na novo predlagan strukturni descriptor molekularne strukturne formule in razdalj. Na osnovi prikazanih rezultatov je možno primerjati uporabnost Wienerjevih (W)-, Szegedovih (Sz)-povezav prve vrste ( ${}^1\chi$ ) in PI indeksov v razvijanju QSPR poliacenov, pri čemer kot korelacijsko lastnost uporabimo hidrofobnost.