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## Facial parity edge colouring

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### Abstract

A *facial parity edge colouring* of a connected bridgeless plane graph is an edge colouring in which no two face-adjacent edges (consecutive edges of a facial walk of some face) receive the same colour, in addition, for each face  $\alpha$  and each colour  $c$ , either no edge or an odd number of edges incident with  $\alpha$  is coloured with  $c$ . From Vizing's theorem it follows that every 3-connected plane graph has a such colouring with at most  $\Delta^* + 1$  colours, where  $\Delta^*$  is the size of the largest face. In this paper we prove that any connected bridgeless plane graph has a facial parity edge colouring with at most 92 colours.

Math Sci Net: [05C15 \(05C10\)](#)

# **Lično parnostno barvanje povezav**

## **Povzetek**

*Lično parnostno barvanje povezav* povezanega ravninskega grafa brez mostov je tako barvanje povezav, v katerem nobeni dve lično-sosednji povezavi (tj. zaporedni povezavi sprehoda po robu kakega lica) nista enake barve, poleg tega pa je za vsako lice  $\alpha$  in vsako barvo  $c$  število povezav incidenčnih z  $\alpha$  in pobarvanih z barvo  $c$  bodisi nič bodisi liho. Iz Vizingovega izreka sledi, da ima vsak 3-povezan ravninski graf barvanje z največ  $\Delta^* + 1$  barvami, kjer je  $\Delta^*$  velikost največjega lica. V članku dokažemo, da ima vsak povezan ravninski graf brez mostov lično parnostno barvanje povezav z največ 92 barvami.