

DYNAMIC PARTICLE SYSTEMS FOR OBJECT STRUCTURE EXTRACTION

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ABSTRACT

A new deformable model based on the use of a particle system is introduced. By defining the local behavior of each particle, the system behaves as an active contour model showing a variable topology and regularization properties. The efficiency of the particle system is illustrated by two applications: the first one concerns the use of the system as a skeleton extractor based on the propagation of particles inside a tree-shaped object. Using this method, it is possible to generate a cartography of structures such as veins or channels. In a second illustration, the system avoids the problem of initialization of a piecewise cubic B-spline network used to straighten curved text lines.

Keywords: deformable models, particle system, snakes, structure extraction.

INTRODUCTION

Deformable models have been widely used since the original definition of snakes or active contours (Kass *et al.*, 1988). Most developments of deformable models deal with boundary detection and feature extraction in 2-D or 3-D images (Cohen, 1991). Basically, the method consists in deforming and moving an initial curve toward a region of interest. The solution is obtained by minimizing the model energy.

The inability to change from a given topology to another is a major drawback of classical deformable models. For this reason, several approaches have been proposed. Topologically adaptable snakes analyse the curve-topology (Mc Inerney and Terzopoulos, 1995) or the surface-topology (Mc Inerney and Terzopoulos, 1997), and include cutting or fusion steps during the evolution. Level set methods consider the curve or the surface as zero values of a higher dimension object (Sethian, 1996). Implicit models act the same way but are generated from predefined primitives (Yahia *et al.*, 1998). A special class of deformable models is represented by particle systems (Szeliski and Tonnesen, 1992) allowing topology changes during the evolution, and providing results involving predefined primitives, as opposed to level set methods.

The next section presents a deformable model based on the definition of a particle system (Angella *et al.*, 1998). This model overcomes classical deformable model drawbacks. The particle system shows the ability

to change its topology and unlike the classical models does not require an initialization close to the solution.

Then, we present two applications of this model. First, a classical application consists in propagating the particles inside a grayscale tree-shaped object. The algorithm simulates the evolution of a system subjected to internal, and external forces. The simultaneous use of particle systems and tree generation allows to extract a linear piecewise, and connected skeleton of the object. The second application concerns the straightening of text lines (Lavialle *et al.*, 2001): the approach considers a piecewise cubic B-spline system where each curve is defined as a particle. The system propagates in the vertical direction from a central position. Internal forces control the expansion of the curve system, whereas external forces drive each curve toward a text line to obtain the global structure of the distorted text.

PARTICLE SYSTEM

Model definition

Let us denote by S a particle system. This system is a set of nodes (or particles) M_i . Each node can evolve in the x-y image plane in response to different acting forces. These forces are divided in two groups: internal, and external forces. Internal forces control, and regulate the expansion of the system; external forces drive evolution of S according to the current image of interest. The behavior of a particle is the consequence of the resulting force exerted on this particle.

Our goal is to encourage the particle system to explore the image. Towards that end, interaction rules between particles have to be defined. A repulsion behavior allows the system to expand; an attractive behavior forces particles not to move away from other particles. Thus, internal forces are defined through the introduction of a Lennard-Jones interaction potential function gathering a long-range attraction term and a short-range repulsion term (Heyes, 1998). Classically, the Lennard-Jones potential describes the interaction between pairs of atoms in a solid or a liquid. It has the following form:

$$\phi(r) = \varepsilon \left[\left(\frac{\sigma}{r} \right)^{12} - \left(\frac{\sigma}{r} \right)^6 \right], \quad (1)$$

where r is the distance from an atom to an any other atom. The constants ε and σ are important in that they determine the strength and shape of the interaction, hence the properties of the solid or liquid. The force between individual atoms is the negative of the potential gradient.

Herein, we consider the following function:

$$\rho(d) = \frac{B}{d^m} - \frac{A}{d^n}, \quad (2)$$

where d is the distance between two particles. A , B , m and n are positive coefficients used to set the equilibrium distance. In our application, we chose $m = 2$, $n = 1$ yielding an equilibrium distance equal to $2B/A$.

Using ρ , we can compute a global interaction force $f_{\text{int}}^{(t,i)}$:

$$f_{\text{int}}^{(t,i)} = - \sum_{M_j \in v_i^{(t)}} \vec{\nabla} \rho(d_{ij}), \quad (3)$$

where $v_i^{(t)}$ is the neighborhood of M_i at step t (the notion of neighborhood will be defined in the next section).

External forces being application-dependent, they will be described (along with additional internal forces) in the next section where two applications are considered.

System evolution

One can control the behavior of each particle M_i by computing F_i , the total resulting force. Then, if we consider that each particle is a mechanical system, its

evolution follows the classical Newtonian mechanical relation:

$$m_i \cdot \frac{dv_i(t)}{dt} = F_i, \quad (4)$$

m_i stands for the mass of the particle. For our purpose, m_i is a constant and can be included in F_i . The numerical integration of this differential equation is obtained using the Euler integration method. This leads to the choice of a time interval parameter, resulting from a precision/computation time compromise. Then, (4) becomes:

$$\begin{cases} v_i^t = v_i^{t-1} + \delta t \cdot (F_i - \alpha_f v_i^{t-1}) \\ x_i^t = x_i^{t-1} + \delta t \cdot v_i^t \end{cases}, \quad (5)$$

where x_i^t and v_i^t are respectively the position and the velocity of a particle M_i at step t . α_f is a friction coefficient added to ensure the stability of the system.

Our approach consider the evolution of the system as a solution of a Newtonian mechanical Eq. 4. Another equivalent approach can be proposed by generating all forces from a unique potential function, so that the evolution of the particle system S will be similar to the process involved when minimizing a global energy, as it is performed when dealing with classical active contour (Kass *et al.*, 1988).

APPLICATIONS OF THE MODEL

Object structure extraction

The problem of skeleton extraction has found many solutions based on mathematical morphology algorithms (Serra, 1982). Here, we propose to extract structures in grayscale tree-like objects by using the particle system described above (Angella *et al.*, 1998).

The evolution of the system is the consequence of a Lennard-Jones interaction force (Eq. 3) complemented with two other internal forces presented in Angella *et al.* (1998) within the framework of object structure extraction.

The first one provides the system with learning abilities: this force, inspired by the so-called evolutionary computation domain, acts as "insect pheromones", driving particles preferentially to the paths already used by prior particles (Dorigo and Gambardella, 1997). To do so, we build a velocity map I_{ph} using the velocity v_i^t of each particle M_i at each step t of the algorithm. This map saves the average of the velocity observed in each pixel p of the

image. Then, we define an elementary pheromonal force averaged around x_i^t as expressed by Eq. 6:

$$f_{ph}^{(t,i)} = \frac{1}{card \Gamma_i^{(t)}} \cdot \sum_{p \in \Gamma_i^{(t)}} (\vec{\nabla} I_{ph})_p, \quad (6)$$

where x_i^t is the position of M_i at step t and $\Gamma_i^{(t)}$ is the given area around x_i^t .

The second additional internal force is a regularization force between particles that tends to align particles within the same branch of a given object by attracting a particle to the middle point of its two neighbors. Let us consider a particle M_i with a neighboring, at step t , $V_i^t = \{M_j, M_k\}$. The force is defined by:

$$f_{reg}^{(t,i)} = \left(\frac{x_j^{(t)} - x_k^{(t)}}{2} - x_i^{(t)} \right), \quad (7)$$

x_j^t, x_k^t and x_i^t are respectively the position of M_j , M_k and M_i at step t .

As we want our system to lie inside objects, we use an external force depending directly on the gradient of the image I , defined as follows:

$$f_{ext} = -k_{ext} \cdot \vec{\nabla} (\|\nabla G * I\|), \quad (8)$$

$\|\nabla G * I\|$ is the modulus of a filtered gradient of the image. G is a low pass filter used to extend the influence area of objects boundaries in I . k_{ext} is used to control this influence.

The particle system will evolve inside objects from an initial location x_{init} where particles are generated with initial velocity v_{init} . The generation is T-periodic (prior to generating a particle, a test is run to avoid overpopulation within the generating area).

The process described above simulates the evolution of a deformable expandable tree created and modified by linking neighboring particles and cutting branches according to different rules defined below. The evolution of the tree T may be viewed as the joint evolution of the particle system S and a set of links L between the elements of S .

Updating the tree carries with it the ability to change the topology. In addition, L is involved in the determination of the neighborhoods V_i^t , and then in

the computation of $f_{int}^{(t,i)}$ and $f_{reg}^{(t,i)}$. These neighborhoods are actually necessary to list particles influencing a given particle. In this respect, the algorithm does not rely on the shape of objects but on their structure as expressed by L .

We define the set of links L with the binary function:

$$l^{(t)} : (i, j) \mapsto \begin{cases} 1 & \text{if } M_i \text{ are linked at step } t \\ 0 & \text{if not} \end{cases}, \quad (9)$$

with $l^{(t)}(i, i) = 0, \forall i$.

Eq. 9 defines the neighborhood of M_i at step t :

$$V_i^t = \{M_j / l^{(t)}(i, j) = 1\}. \quad (10)$$

The search for a neighbor of M_i is performed with respect to the trajectory of M_i and includes time and space constraints: the neighbor shall be the closest to a previous location of M_i . The entire trajectory of M_i is accordingly scanned starting at step t down to step 1 using a restricted area around the trajectory. The selected neighbor M_j is obtained using the following algorithm:

for $m=t, \dots, 1$:

$$j = \arg \min_{k / M_k \in S} (\|x_k^t - x_i^m\|)$$

$$\text{if } (\|x_j^t - x_i^m\|) \leq D_\varepsilon$$

then $M_j \in V_i^t$ break

else $m=m-1$

end if

D_ε restricts the search process around the trajectory of M_i and m denotes the current iteration varying from t down to 1. The process is stopped at iteration m if a neighbor satisfying the proximity condition is found.

Updating the tree modifies the structure of the links at every step of the evolution of S . Links between particles are dynamically changed according to the geometric relations between them and taking advantage of the previous trajectories of particles. We analyze different cases corresponding to different configurations for each particle: addition and convergence, deletion, divergence and shift:

- Addition and convergence: when a particle has an empty neighborhood, a neighbor must be found among the other particles using the algorithm above. This situation happens for a newly generated particle or for a particle whose links are cut to remain consistent with the object structure. In addition, the system can hold optional convergence cases, leading to cycle generations, so that the tree becomes a graph including loops.
- Deletion: if a particle M_i moves too far away from its neighbors, its links must be cut. The deletion process is just based on a deletion distance.
- Divergence and shift: the divergence, or shift behavior, occurs around a junction in the object structure. To understand how the tree is updated, let us analyze Fig. 1. In the vicinity of a junction (step a), the particle M_2 does not follow the particle M_1 , so that at step b the structure of the links in L does not reflect the structure of the object. At step c, we decide to cut all links to M_2 and to suitably reconnect the tree at step d. This topology change is tractable if one finds a criterion to decide when cutting the skeleton at step c. The rule adopted is based on angle comparisons considering that the angle between two links associated to a given particle has to be greater than a fixed minimal angle θ_{junction} . If it is not the case, a junction is detected, the two links

are removed and new links have to be found leading to a topology change.

This simultaneous evolution of S and L allows a hierarchical exploration of the object and overcomes the topology changes problem. Finally, the approach returns a hierarchical, connected, and piecewise linear “skeleton” of the object without any post-processing.

Fig. 2 illustrates the evolution of the system on a synthetic tree-like object. In this case, all particles are generated at the same location with the same initial velocity vector. The tree update process consists in adding, deleting or shifting links according to the geometric relations between the particles and taking the trajectories into account (Angella *et al.*, 1998). In this example, the evolution stops because of the initialization vicinity test.

Fig. 3 shows a result obtained on a more complex image. The simultaneous use of a particle system and tree generation yields the skeleton of the river in an aerial image. The particles are generated from the top-left of the structure and are then allowed to explore the object. Fig. 3a and 3b show the trajectories of the particles and the resulting structure, respectively. Note that some ramifications are not explored: some image areas do not provide the particles with relevant external forces due to a low contrast between the object and its environment. In addition, the object structure may become too thin at the end of a ramification to allow the extension of the system.

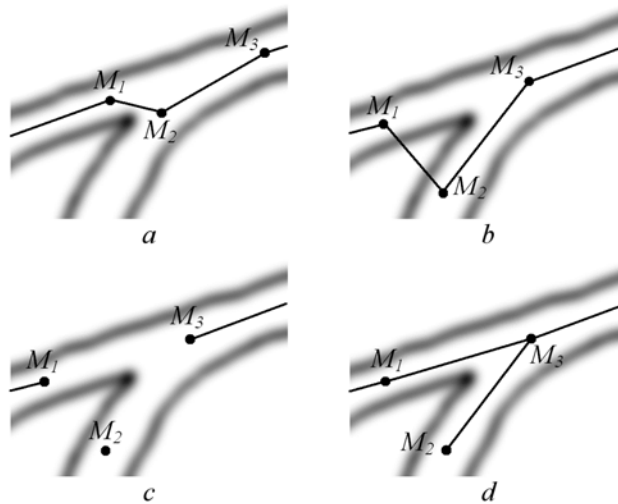


Fig. 1. Links update in the divergence-shift case. Particles are moving from right to left.

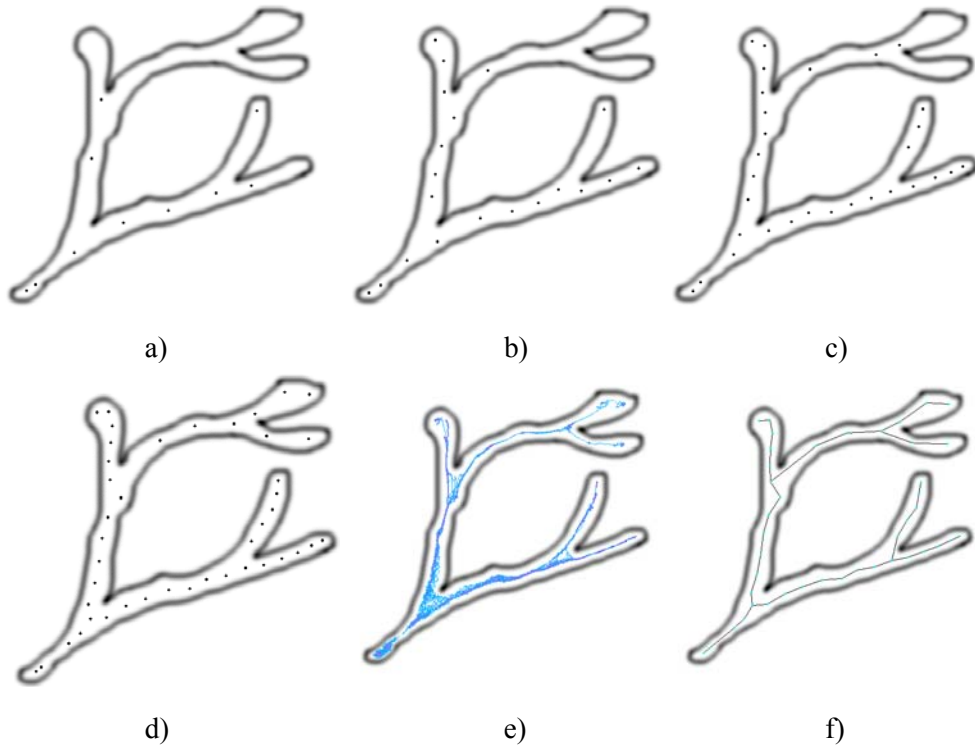


Fig. 2. Synthetic tree-like object. 2a, 2b, 2c and 2d: Evolution of the particle system. 2e: Particle trajectories. 2f: final tree

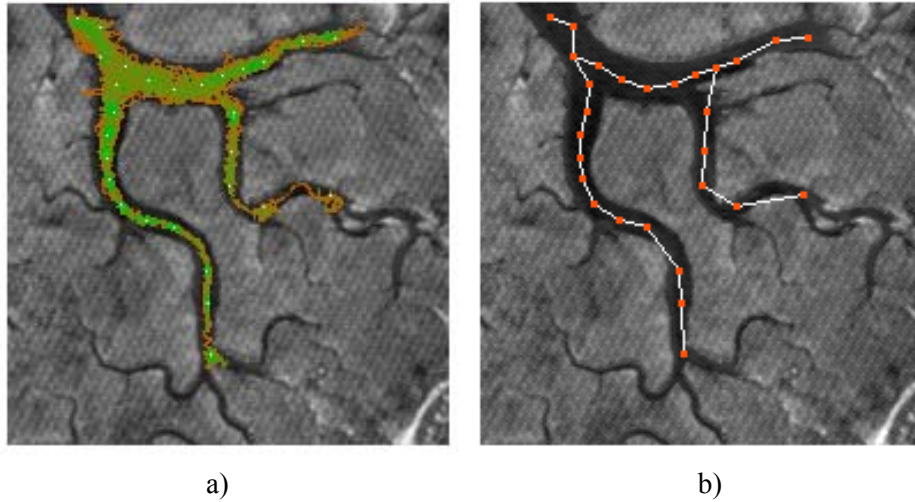


Fig. 3. Real tree-like object structure extraction. 2a) particle trajectories. 2b) main ramifications of the skeleton for an aerial image.

ACTIVE CONTOURS NETWORK TO STRAIGHTEN DISTORTED TEXT LINES

We proposed a 2D extension of the system to straighten distorted text (Fig. 4a) (Lavialle *et al.*, 2001). For such a purpose, the system of particles is transformed into a system of curves. A curve is associated to each line of text. Noting a_i^k the k^{th} parameter of a i^{th} curve C_i , our goal is to define an energy function depending on a_i^k . Using a classical approach, each curve may be modeled by Basis

splines (B-splines) (Lehmann *et al.*, 1999). Here, we rather use piecewise cubic B-splines (i.e. each curve is a set of connected cubic B-splines). Let us note C_i a B-Spline. $a_i^{k,s}$ is then the k^{th} control point of the s^{th} connected spline of C_i . The model continuity is enforced by constraining the control points in order to obtain smoothed curves (Lavialle *et al.*, 2001).

The horizontal coordinate of each parameter $a_i^{k,s}$ is fixed, and the value of $a_i^{k,s}$ yields the vertical

position of the s^{th} spline of C_i . The internal energy is defined by assuming that the text is locally uniform (i.e. line spacing is constant). Thus, our purpose is to move each curve toward the centre of its two neighbors:

$$E_{int}^{k,s}(i) = \left[a_i^{k,s} - \frac{1}{2}(a_{i-1}^{k,s} + a_{i+1}^{k,s}) \right]^2. \quad (11)$$

The system evolves along the vertical direction from an initial location. In addition to the internal energy defined above, we introduce an interaction force based on a Lennard-Jones potential between the control points of neighboring curves to force them to move from their initial location.

The minimization of an appropriate external energy will allow to attract the curves toward the text. The computation of this energy is based on a mathematical morphology transformation: we first use an opening on the original image to fill in spaces between letters. Fig. 4b shows the result obtained with a structuring element of size 11×5 . Then, considering the bottom of the lines, the external energy is computed using a vertical Deriche gradient

(Deriche, 1987). The smoothing resulting from the use of this operator is necessary to extend the influence of the lines, and then to attract the curves toward the solution

Fig. 4c shows the value of the vertical gradient ∇I_y . Finding the bottom of the lines is done with a very simple energy functional: $E_{ext} = -\nabla I_y$ leading to the external force:

$$f_{ext} = k_{ext} \cdot \vec{\nabla}(\nabla I_y). \quad (12)$$

All curves are generated at an initial location y_{init} with an initial velocity v_{init} . The evolution of the system follows the classical mechanical relation described in the previous section.

Fig. 5 shows an example of distorted text. Fig. 6 illustrates the evolution of the curve system on a detail of Fig. 5. The curves are initialized at the middle of the page. After 150 iterations, each curve system has converged toward a text line and the straightening is possible (Fig. 7).

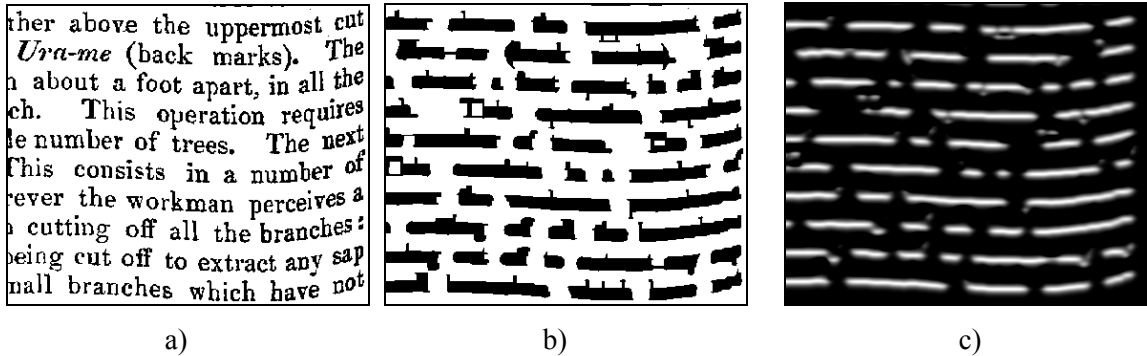


Fig. 4. a) curved text, b) opening of 4a, c) vertical gradient computed from 4a.

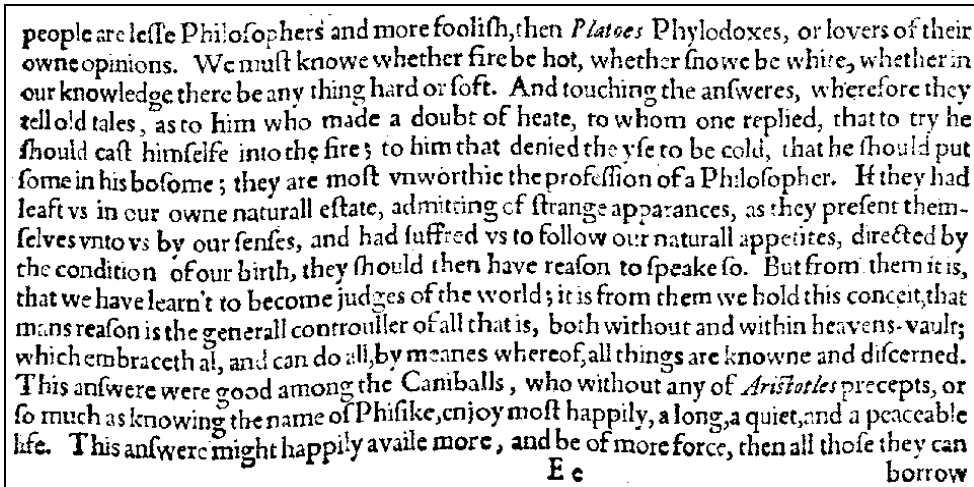


Fig. 5. Example of distorted text.

nd more foolish, then *Platoes* Phylodox we whether fire be hot, whether snowe ng hard or soft. And touching the answ ade a doubt of heate, to whom one r re; to him that denied the yfe to be col most vnworthie the profession of a Philo late, admitting of strange apparances, d had suffred vs to follow our naturall a y should then have reason to speake fo. judges of the world; it is from them we rrouler of all that is, both without and v all, by meanes whereof, all things are kn g the Caniballs, who without any of d Phisike, enioy most happily, a long, a c ly availe more, and be of more force, t
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a

nd more foolish, then *Platoes* Phylodo we whether fire be hot, whether snowe ng hard or soft. And touching the answ ade a doubt of heate, to whom one r re; to him that denied the yfe to be col most vnworthie the profession of a Philo late, admitting of strange apparances, d had suffred vs to follow our naturall a y should then have reason to speake fo. judges of the world; it is from them we rrouler of all that is, both without and v all, by meanes whereof, all things are kn g the Caniballs, who without any of d Phisike, enioy most happily, a long, a ly availe more, and be of more force, t
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more foolish, then *Platoes* Phylodox whether fire be hot, whether snowe ard or soft. And touching the answ a doubt of heate, to whom one t to him that denied the yfe to be col vnworthie the profession of a Philo admitting of strange apparances, d suffred vs to follow our naturall a ould then have reason to speake fo. ges of the world; it is from them we ler of all that is, both without and v y meanes whereof, all things are kn e Caniballs, who without any of d hifike, enioy most happily, a long, a vaile more, and be of more force, t
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more foolish, then *Platoes* Phylodo whether fire be hot, whether snowe ard or soft. And touching the answ a doubt of heate, to whom one t to him that denied the yfe to be col vnworthie the profession of a Philo admitting of strange apparances, d suffred vs to follow our naturall a ould then have reason to speake fo. ges of the world; it is from them we ler of all that is, both without and v y meanes whereof, all things are kn e Caniballs, who without any of d hifike, enioy most happily, a long, a vaile more, and be of more force, t
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Fig. 6. Evolution of a curve system.

people are lesse Philosophers and more foolish, then *Platoes* Phylodoxes, or lovers of their owne opinions. We must knowe whether fire be hot, whether snowe be white, whether in our knowledge there be any thing hard or soft. And touching the answeres, wherefore they tell old tales, as to him who made a doubt of heate, to whom one replied, that to try he should cast himselfe into the fire; to him that denied the yfe to be cold, that he should put some in his bosome; they are most vnworthie the profession of a Philosopher. If they had leaft vs in our owne naturall estate, admitting of strange apparances, as they present themselves vnto vs by our senses, and had suffred vs to follow our naturall appetites, directed by the condition of our birth, they should then have reason to speake so. But from them it is, that we have learnt to become judges of the world; it is from them we hold this conceit, that mans reason is the generall controuler of all that is, both without and within heavens-vault; which embraceth al, and can do all, by meanes whereof, all things are knowne and discerned. This answer were good among the Caniballs, who without any of *Aristotles* precepts, or so much as knowing the name of Phisike, enioy most happily, a long, a quiet, and a peaceable life. This answer might happily availe more, and be of more force, then all those they can
E e borrow

Fig. 7. Straightened text.

DISCUSSION

In this paper, we presented a particle system acting as a deformable model with flexible topology and regularization properties. When applied to the extraction of an object structure, the system returns a continuous and piecewise connected skeleton. As the particles first move through large ramifications, the method can give additional information on the hierarchy of structures. We can notice that the 3-D extension of this method is obvious: it has been already successfully tested on synthesized 3-D images.

In the second application, we demonstrated the ability of our method to simplify the initialization step in the case of a system of cubic B-splines used to straighten text lines.

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