

## OPTIMIZING THE PARAMETERS FOR FRICTION WELDING STAINLESS STEEL TO COPPER PARTS

### OPTIMIRANJE PARAMETROV PRI TORNEM VARJENJU NERJAVNEGA JEKLA NA BAKRENE DELE

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St-Cu (stainless steel and copper) parts were friction welded with the aim to optimize the process parameters in the present study. The joints obtained with various process-parameter combinations were subjected to a tensile test. Empirical relationships were developed to predict the strength of the joints using RSM (the response-surface methodology) and the coherency of the model was tested. The tensile properties, microhardness variations, SEM, the EDS analysis and X-ray diffraction (XRD) analysis of the welded specimens were evaluated. It was found, with an ANOVA analysis, that the friction pressure/friction time relation has the largest influence on the tensile strength of the joints followed by the rotational speed. However, it was also found that the formation of intermetallics at the interface is responsible for a higher hardness and lower tensile strength of the friction-welded stainless steel-copper joints.

Keywords: friction welding, metallurgy, response-surface methodology, tensile strength

V predstavljenem delu so bili deli St-Cu (nerjavno jeklo in baker) torno varjeni z namenom optimizacije procesnih parametrov. Spoji, dobljeni z različnimi procesnimi parametri, so bili preizkušeni z nateznim preizkusom. Razvite so bile empirične odvisnosti za napovedovanje trdnosti spojev s pomočjo RSM (Metodologija odgovora površine) in izvršena je bila koherenca modela. Ocenjene so bile natezne lastnosti, spreminjanje mikrotvrdote, SEM, EDS analiza in rentgenska difrakcija (XRD) zvarjenih vzorcev. Iz ANOVA analize je bilo ugotovljeno, da ima torni tlak/čas trenja največji vpliv na natezno trdnost spojev, sledi pa mu hitrost vrtenja. Ugotovljeno je bilo, da je večja trdota in manjša natezna trdnost tornu varjenih spojev posledica nastanka intermetalne zlitine na stiku nerjavno jeklo-baker.

Ključne besede: tornu varjenje, metalurgija, metodologija odgovora površine, natezna trdnost

## 1 INTRODUCTION

Parts made of different materials are known to be cost-effective. The life cycle of the materials, especially in corrosive media, is prolonged. Many ferrous and non-ferrous alloys can be friction welded. Friction welding can be used to join metals of widely different thermal and mechanical properties. The combinations that can be friction welded cannot be joined with other welding techniques because of the formation of brittle phases that make the joint poor with respect to mechanical properties. Friction welding prevents distortion of the materials, as heat is not applied.

The welding technology is widely used in manufacturing. The development of new welding methods gained importance along with the developing technology.<sup>1-4</sup> Welding of different metals and their alloys is a common application in engineering solutions. Fusion welding is almost impossible in such cases due to incompatible physical characteristics and chemical compositions of different metals and alloys. As a result, friction welding was developed. Several researches worked on the heat in friction welding.<sup>5-7</sup> In friction welding, heat is generated at the interface of the workpieces since mechanical energy is dissipated as heat during the rotation under

pressure. Friction welding is a solid-state welding process, using the heat generated through the mechanical friction with a moving workpiece, with an addition of an upsetting pressure to plastically displace the material. Friction welding is generally used to join the parts that are axially symmetrical and have circular cross-sections. However, it can be easily used to join parts without circular cross-sections, with the aid of automation devices and computerized control facilities.<sup>8</sup> It is an energy saver since heat is not applied.

The friction time and pressure, the upset time and pressure and the speed of rotation are the principal variables in friction welding.<sup>9-12</sup> There are two types of friction-welding techniques: continuous-drive friction welding and inertia friction welding. Different metals have different hardness values and different melting points. Interface activity during friction welding forms brittle intermetallic phases or eutectics with low melting points. Clean welding surfaces are also of prime importance.<sup>13-15</sup> In welded St-Cu joints, the joint strength increases with the increasing upset pressure up to the critical value. An increase in the friction time causes a lower strength of a St-Cu joint compared to the Cu base metal.<sup>16</sup> A deformation of the material during friction welding is generally due to the diffusion involving a

migration of lattice defects, which can be influenced by an external electric field.<sup>17</sup> Sintered powder metallurgical preforms have a low mass, high stiffness and, therefore, their natural frequency is high. Having inherent porosity, they can also be good dampeners besides possessing the latent lubricant.<sup>18</sup> Maalekian<sup>19</sup> found that the formation of hard interlayers, such as intermetallic phases, when joining dissimilar materials may cause a joint to become brittle. Further, Sahin et al.<sup>20,21</sup> showed that the intermetallic phases formed in the interface cause a decrease in the strength of the joints.

However, based on the literature review, Murti and Sundaresan<sup>22</sup> carried out a study about a parameter optimization using a statistical approach based on factorial-experiment-design friction welding of dissimilar materials. The response-surface methodology (RSM) is a collection of mathematical and statistical techniques that are useful for designing a set of experiments, developing a mathematical model, analyzing the optimum combination of the input parameters and graphically expressing the values.<sup>23</sup> To obtain the maximum strength, it is essential to have complete control over the relevant process parameters as demonstrated.<sup>24</sup>

Therefore, in this work, an attempt was made to optimize the process parameters of continuous-drive friction welding to achieve the maximum tensile strength of stainless steel-copper parts using the response-surface methodology. Tensile tests were performed on the welded test parts. A microstructure analysis, EDS analysis, XRD analysis and microhardness variations were also carried out on the test parts.

## 2 EXPERIMENTAL WORK

In the experiments, AISI 304 austenitic stainless-steel and copper parts having a diameter of 10 mm were made

using the continuous-drive friction-welding process parameters. The chemical composition and mechanical properties of the stainless-steel and copper parts are presented in **Tables 1** and **2**, respectively, as given in<sup>25</sup>.

Different combinations of the process parameters were used to carry out the trial runs. Process parameters were tested by varying one of the factors while keeping the rest of them at constant values. The working range of each process parameter was determined for a smooth appearance without any observable defects. The selected levels of the process parameters and design matrix with their units and notations are presented in **Tables 3** and **4**.

However, in order to examine the intermetallic phases formed at the interface of the joints, SEM (scanning electron microscopy) and EDS (energy-dispersive X-ray spectroscopy) were applied to the joints. Examinations were carried out with an SEM-JEOL JSM 5410 LV microscope and in the field of 200 kV. In addition, the weld zones of the joints were analyzed in this work since an XRD analysis of the phase constituents in the weld zone is of a great importance.

Then, the strength of the joints was related to the hardness variation within the HAZ. The hardness variations across the welding regions of the joints were measured using a 0.3 kg load Vickers microhardness test.

## 3 RESULTS AND DISCUSSION

### 3.1 Empirical relationships and the optimization

The responses, the tensile-strength (*TS*) values of friction-welded joints, are the functions of the friction-welding parameters such as the friction pressure per second (*F*), the forging pressure per second (*D*) and the rotational speed per second (*N*) and they can be expressed as:

**Table 1:** Chemical composition of austenitic stainless steel used in the experiment<sup>25</sup>

**Tabela 1:** Kemijska sestava avstenitnega nerjavnega jekla, uporabljenega pri preizkusu<sup>25</sup>

Material	% C	% P	% S	% Mn	% Si	% Cr	% Ni	Tensile strength (MPa)
AISI 304 (X5CrNi1810)	< 0.07	< 0.045	< 0.030	< 2.0	< 1.0	17–19	8.5–10.5	825

**Table 2:** Chemical composition of copper used in the experiment

**Tabela 2:** Kemijska sestava bakra, uporabljenega pri preizkusu

Copper	% Sn	% Pb	% Zn	% P	% Mn	% Fe	% Ni	% Si	% Mg	% Al	% Bi	% S	% Sb	% Cu	Tensile strength (MPa)
	0.00222	<0.0020	<0.0010	0.00137	<0.0005	0.0381	<0.0010	0.00745	0.00376	0.00500	<0.0005	0.00251	<0.0020	99.93	300

**Table 3:** Feasible working limits of friction-welding parameters

**Tabela 3:** Območje delovnih parametrov pri tornem varjenju

Parameter	Notation	Unit	Level				
			-1.68	(-1)	(0)	(+1)	+1.68
Friction pressure/Friction time	<i>F</i>	MPa/s	3.78	5.82	8.82	11.82	13.86
Upset pressure/Upset time	<i>D</i>	MPa/s	2.96	5	8	11	13.04
Rotational speed/sec	<i>N</i>	s <sup>-1</sup>	18.46	20.5	23.5	26.5	28.54

**Table 4:** Design matrix and the corresponding output response  
**Tabela 4:** Postavljena matrika in ustrezni dobljeni odgovori

Standard order	Run order	Original value			Tensile strength (MPa)
		F	D	N	
16	1	8.82	8	23.5	223
18	2	8.82	8	23.5	222
4	3	11.82	11	20.5	190
9	4	3.78	8	23.5	150
20	5	8.82	8	23.5	218
6	6	11.82	5	26.5	210
15	7	8.82	8	23.5	223
1	8	5.82	5	20.5	130
7	9	5.82	11	26.5	213
5	10	5.82	5	26.5	180
8	11	11.82	11	26.5	215
12	12	8.82	13.04	23.5	217
11	13	8.82	2.96	23.5	160
10	14	13.86	8	23.5	216
3	15	5.82	11	20.5	150
19	16	8.82	8	23.5	222
17	17	8.82	8	23.5	219
13	18	8.82	8	18.46	200
14	19	8.82	8	28.54	215
2	20	11.82	5	20.5	195

$$TS = f \{F, D, N\} \quad (1)$$

The second-order polynomial (regression) equation used to represent the response surface  $Y$  ( $TS$ ) is as follows:

$$Y = b_0 + \sum b_i x_i + \sum b_{ii} x_i^2 + \sum b_{ij} x_i x_j \quad (2)$$

and for three factors, the selected polynomial could be expressed as:

$$TS = b_0 + b_1(F) + b_2(D) + b_3(N) + b_{12}(FD) + b_{13}(FN) + b_{23}(DN) + b_{11}(F^2) + b_{22}(D^2) + b_{33}(N^2) \quad (3)$$

Regression coefficients are  $b_1, b_2, b_3, \dots, b_{44}$  where  $b_0$  is the average of the responses and they depend on the respective linear, interaction and squared terms of the factors as shown in<sup>26,27</sup>. The significance of each coefficient was determined with a  $t$ -test and  $p$ -values, listed in **Table 5**.

The value of a coefficient was calculated using the Design-Expert software. The values of the probability  $>F$  of less than 0.05 indicate that the model terms are significant. In this case,  $F, D, N, FD, FN, DN, F^2, D^2$  and  $N^2$  are significant model terms. The values greater than 0.1 point out that the model terms are not significant. The results of multiple linear regression coefficients for the second-order response surface model are given in **Table 6**.

The final empirical relationship was obtained using only these coefficients, and the developing final empirical relationship for the tensile strength is given below:

$$TS = [221.36 + 18.16F + 10.90D + 13.05N - 6.62FD - 9.12FN + 2.88DN - 14.74F^2 - 12.80D^2 - 6.08N^2] \quad (4)$$

**Table 5:** ANOVA test results for the response of the tensile strength  
**Tabela 5:** Rezultati ANOVA preizkusa za odgovore natezne trdnosti

Source	Sum of squares	df	Mean square	F-value	P-value prob > F	significant
Model	14726.69	9	1636.30	13.39	0.0002	
A-F	4503.47	1	4503.47	36.85	0.0001	
B-D	1622.62	1	1622.62	13.28	0.0045	
C-N	2325.93	1	2325.93	19.03	0.0014	
AB	351.12	1	351.12	2.87	0.1209	
AC	666.12	1	666.12	5.45	0.0417	
BC	66.13	1	66.13	0.54	0.4789	
A^2	3132.15	1	3132.15	25.63	0.0005	
B^2	2360.38	1	2360.38	19.31	0.0013	
C^2	532.80	1	532.80	4.36	0.0633	
Residual	1222.11	10	122.21			
Lack of fit	1199.28	5	239.86	52.52	0.0003	
Pure error	22.83	5	4.57			
Cor. total	15948.80	19				
Std. dev.	11.05		R-squared		0.9234	
Mean	198.40		Adj. R-squared		0.8544	

**Table 6:** Estimated regression coefficients

**Tabela 6:** Ocenjeni regresijski koeficienti

Factor	Estimated regression coefficients
	Tensile strength (MPa)
Intercept	221.36
F-friction force/friction time	18.16
D-upset force/upset time	10.90
N-rotational speed	13.05
FD	-6.62
FN	-9.12
DN	2.88
F <sup>2</sup>	-14.74
D <sup>2</sup>	-12.80
N <sup>2</sup>	-6.08

The ANOVA (analysis of variance) technique was used to check the adequacy of the developing empirical relationship. In this investigation, the desired level of confidence was taken to be 95 %. The relationship is considered adequate if the calculated  $F$ -value of the model developed does not go over the standard tabulated  $F$ -value and the calculated  $R$ -value of the developed relationship exceeds the standard tabulated  $R$ -value for a desired level of confidence. It was found that the above model is adequate. In the same way, interactions  $FD, FN, DN$  had significant effects. A lack of fit was not significant though it was desired. The normal probability plot of the residuals for the tensile strength is shown in **Figure 1**. It reveals that the residuals are on a straight line, which means that the errors are distributed normally. Each predicted value matches well its experimental value, as shown in **Figure 2**. The response-surface methodology (RSM) was used to optimize the friction-welding parameters in this study. The response contours can assist in the prediction of the response for any zone in the experimental field as observed in<sup>24,25</sup>.

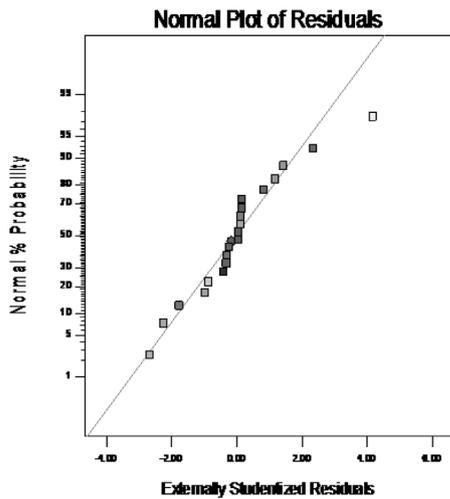


Figure 1: Normal probability plot of residuals  
Slika 1: Normalna verjetnost izrisa ostankov

The end of the response plot shows the maximum achievable tensile strength. Figures 3 and 4 show that the tensile strength increases with the increasing friction pressure/time relation and rotational speed and then it decreases.

The maximum tensile strength of the friction-welded joints was attained under the following welding conditions: a friction pressure/time relation of 8.82 MPa/s (a friction pressure of 75 MPa and a friction time of 8.5 s), an upset pressure/time relation of 8 MPa/s (an upset pressure of 160 MPa and an upset time of 20 s) and a rotational speed of and 23.5 s<sup>-1</sup>, showing the accuracy of the model.

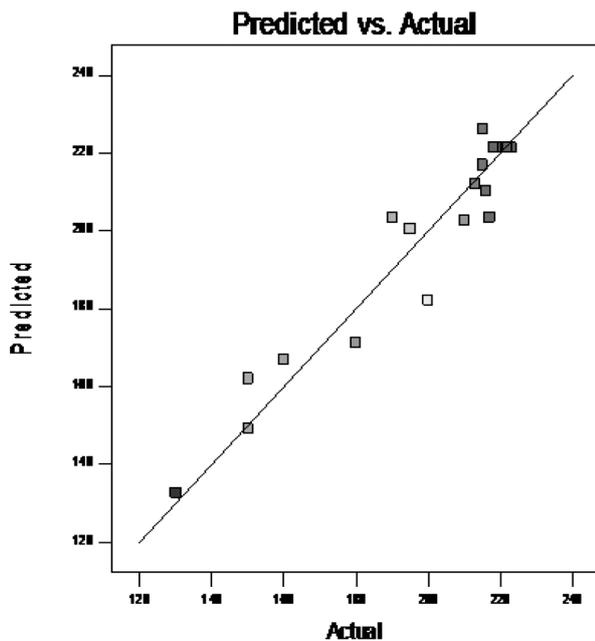


Figure 2: Correlation graph of the response  
Slika 2: Prikaz korelacije odziva

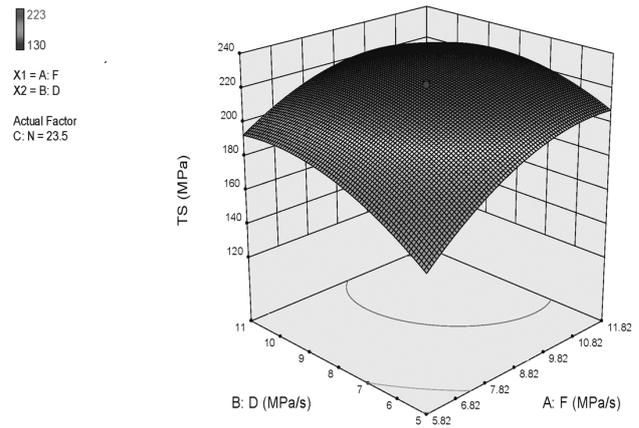


Figure 3: Response plots of the process parameters for the tensile strength  
Slika 3: Prikaz odziva procesnih parametrov na natezno trdnost

During the welding processes, the strength of the welds obtained with dissimilar materials strongly depends on the temperature attained by each substrate. Differences in the mechanical and thermophysical properties and behaviour of the substrates at the interface influence the quality of the joints during the welding as reported in<sup>20,21</sup>.

### 3.2 Metallurgical analysis

The macrophotography of the joints is given in Figure 5. There is no evidence of cracking or other defects in the joints. Due to the variations in the strength of the materials, an appreciable variation in the width of the HAZ (heat-affected zone) region is evident from the joints. However, the microstructure of stainless steel is characterized by equiaxed grains, in the austenitic-grain structure being the natural structure of this type of steel at room temperature (Figure 6).

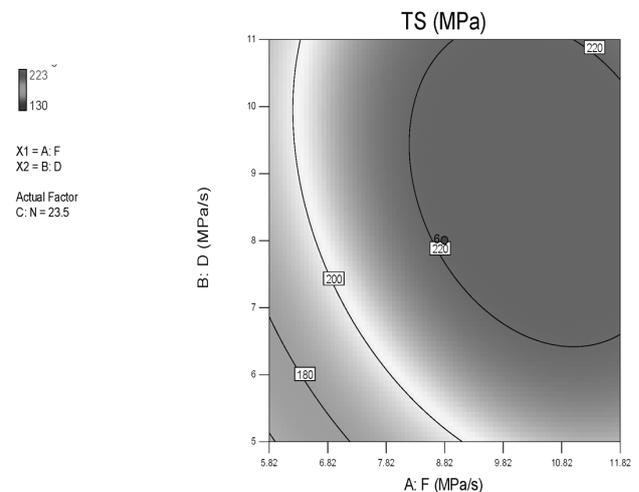
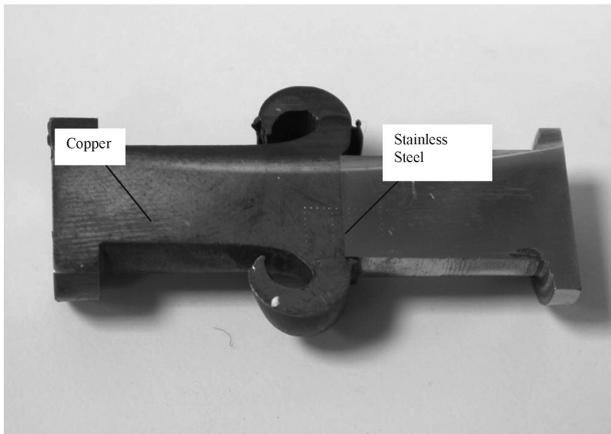
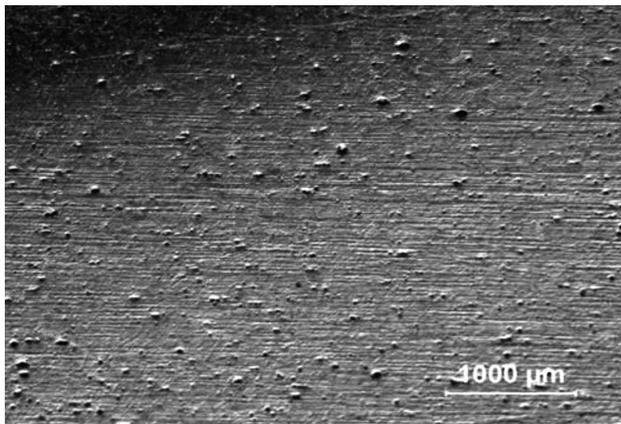


Figure 4: Contour plots of the process parameters for the tensile strength  
Slika 4: Prikaz obrisov procesnih parametrov na natezno trdnost

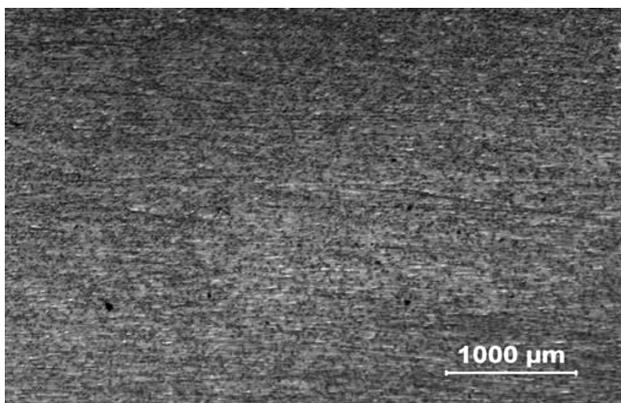


**Figure 5:** Macrophotography of a joint  
**Slika 5:** Makroposnetek spoja

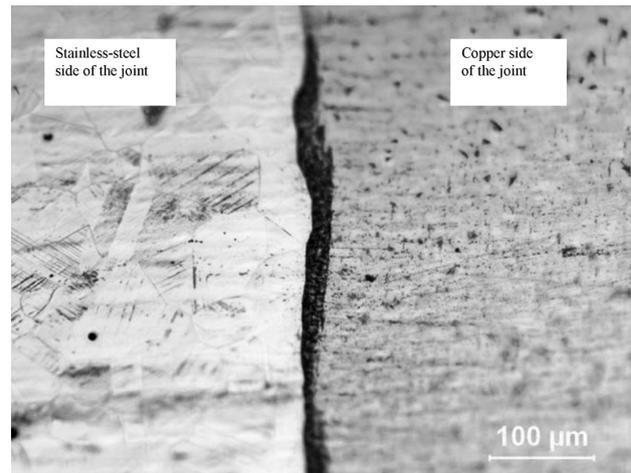
However, copper is formed of eutectic particles, having dark points indicating that it is a mixture of pure copper and cuprous oxide, dispersed in the ground copper (Figure 7). The effect of melting was minimal at the interface because the heat-affected zone (HAZ) was small (Figure 8).



**Figure 6:** Microstructure of stainless steel  
**Slika 6:** Mikrostruktura nerjavnega jekla



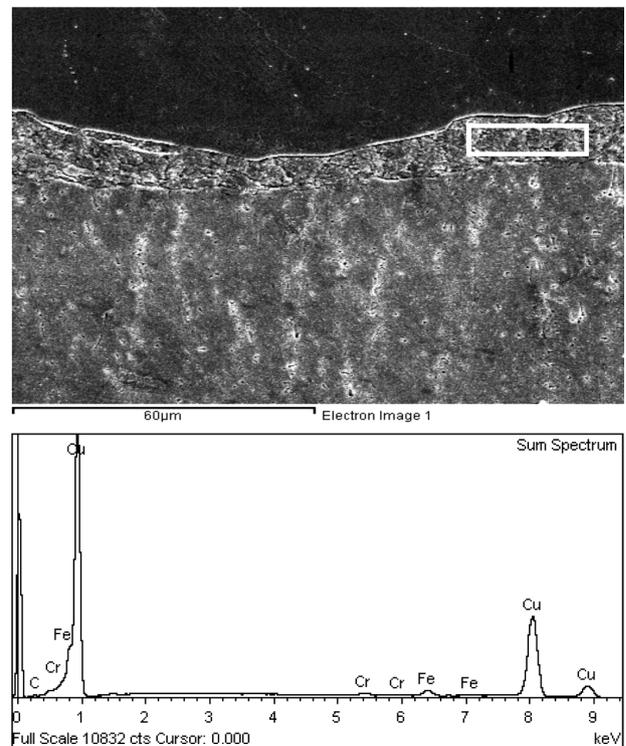
**Figure 7:** Microstructure of copper  
**Slika 7:** Mikrostruktura bakra



**Figure 8:** Image of the interface of a joint  
**Slika 8:** Posnetek stika v spoju

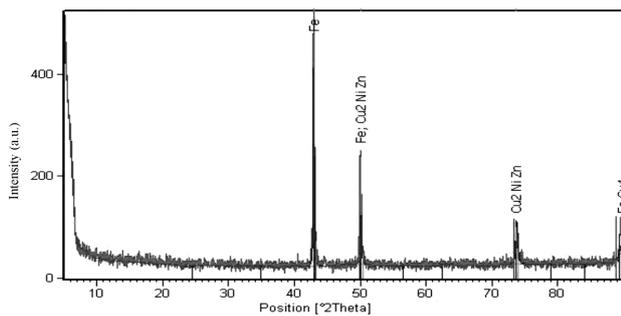
It is also observed that the joints have larger deformations on the Cu side compared to the steel side (Figure 5). Welding flashes occur on the copper side of the interface because the melting temperature of copper is lower than the melting temperature of steel. However, stainless steel does not undergo an extensive deformation while copper undergoes an extensive melting because of the high generated and concentrated frictional heat.

Since copper has a higher thermal conductivity than steel, the heat-affected zone on the copper side is wider



**Figure 9:** EDS analysis of the intermetallic-phase zone of a joint: a) SEM, b) EDS spectrum

**Slika 9:** EDS-analiza intermetalne faze na stiku: a) SEM, b) EDS spekter



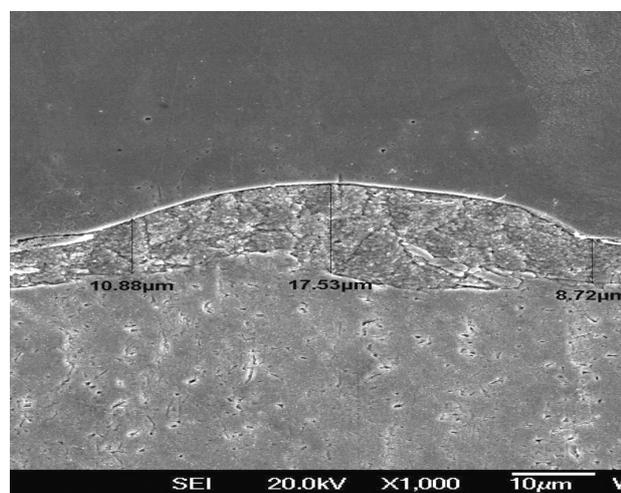
**Figure 10:** XRD results for the welding zone of a joint  
**Slika 10:** Rezultati rentgenske analize (XRD) v zvaru stika

**Table 7:** EDS analysis of the defined zone at the interface  
**Tabela 7:** EDS-analiza označenega področja na stiku

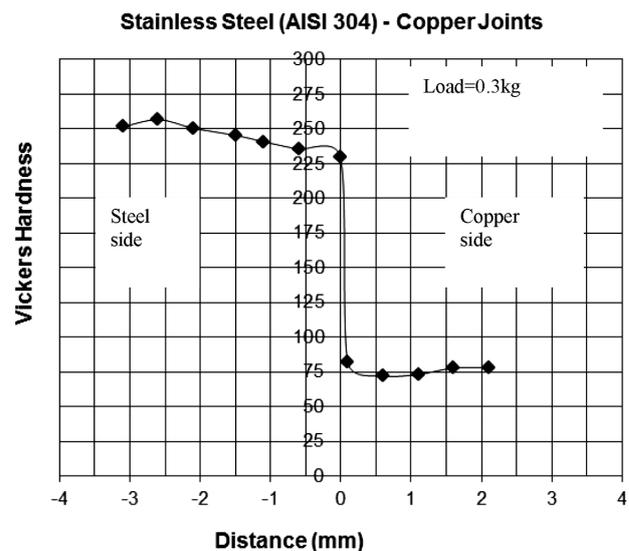
Element	(w%)	(x%)
C	2.70	12.72
Cr	0.98	1.07
Fe	2.96	3.00
Cu	93.36	83.21
Total	100.00	

than that of the steel side. There is no change in the grain size on the steel side. The presence of small particles on the copper side reveals hardening on this side. There are equiaxed  $\alpha$  grains and  $\text{Cu}_2\text{O}$  particles on the copper side. The interface elements of both materials diffused along the interface and some intermetallic phases were formed at the interface as reported in<sup>20,21</sup>.

The EDS analysis performed at a defined zone of the interface showed that the interface was formed of 2.70 % C, 0.98 % Cr, 2.96 % Fe and 93.36 % Cu (**Table 7**). Thus, the presence of intermetallic phases at the interface is obvious. Copper-oxide films were broken into pieces due to an excessive deformation at the interface caused by the rotation (**Figure 9**). According to **Figure 10**, the X-ray diffraction results for friction-welded stainless steel-copper joints indicated that  $\text{FeCu}_4$  and



**Figure 11:** Thicknesses of the intermetallic phases at the interface  
**Slika 11:** Debelina intermetalnih faz na stiku



**Figure 12:** Microhardness variation across the joint  
**Slika 12:** Spreminjanje mikrotrdotne preko spoja

$\text{Cu}_2\text{NiZn}$  intermetallics were formed in the welding zone. The thickness of the layer containing the intermetallic phases varied between 8.72  $\mu\text{m}$  and 17.53  $\mu\text{m}$  (**Figure 11**).

### 3.3 Microhardness measurement

The microhardness of a joint was measured across the weld region and the values were plotted as shown in **Figure 12**. The microhardness is maximum at the interface; this may be due to the formation of brittle intermetallics, and it is one of the reasons for a lower tensile strength of dissimilar joints.

## 4 CONCLUSIONS

Stainless-steel and copper parts were successfully friction joined in this work. The following important conclusions were obtained from this investigation:

- Empirical relationships were developed to predict the tensile strength of the friction-welded stainless-steel and copper parts incorporating process parameters at a 95 % confidence level. The friction-welding parameters were optimized with the response-surface methodology to attain the maximum tensile strength.
- The maximum tensile strength of 223 MPa was attained in the friction-welded joints under the following welding conditions: a friction pressure/time relation of 8.82 MPa/s, an upset pressure/time relation of 8 MPa/s and a rotational speed of 23.5  $\text{s}^{-1}$ .
- The friction pressure/friction time relation was found to have the greatest influence on the tensile strength of the joints, followed by the rotational speed.
- Various intermetallic phases such as  $\text{FeCu}_4$  and  $\text{Cu}_2\text{NiZn}$  occurred at the interface. The formation of intermetallics at the interface is responsible for the

higher hardness and lower tensile strength of the friction-welded stainless steel-copper joints.

- The intermetallic phases at the interface are also expected to play a role in the hardness variations.

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